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# NAVAL POSTGRADUATE SCHOOL

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## THESIS

A COMPUTER PROGRAM FOR SOLVING THE PARABOLIC EQUATION  
USING AN IMPLICIT FINITE-DIFFERENCE SOLUTION METHOD  
INCORPORATING EXACT INTERFACE CONDITIONS

by

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September 1983

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A Computer Program for Solving the Parabolic Equation Using  
an Implicit Finite-Difference Solution Method and  
Incorporating Exact Interface Conditions

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# ABSTRACT

An Implicit Finite-Difference (IFD) program that incorporates exact interface conditions has been developed for solving the parabolic equation. The model preserves continuity of pressure and continuity of the normal component of particle velocity at the interface between media having different sound speeds and densities. Interface conditions are preserved for horizontal and sloping interfaces along a user-specified bottom profile. Test cases are included to demonstrate the use of the model.

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## I. INTRODUCTION

Since its introduction to the underwater acoustics community (Hardin and Tappert, 1973), the parabolic wave equation has stimulated a considerable amount of interest. The first solution programs used a split-step fast Fourier transform method to solve the parabolic equation; however, other solution techniques have been developed (McDaniel and Lee, 1982). One of the motives for developing alternative solution techniques is that problems arise when the Fourier transform encounters an interface between two media having different sound speeds or densities (Lee and Botseas, 1982).

One alternative solution technique uses an implicit finite-difference (IFD) solution method. The IFD method is unconditionally stable and has the capability to incorporate desired interface conditions. Implicit finite-difference methods for solving parabolic equations have been studied extensively by many authors.

A computer program that utilizes the IFD method to solve the parabolic equation has been developed and is examined in detail in this thesis. The computer program predicts acoustic propagation loss in environments having user-specified bottom profiles. The program preserves continuity of pressure and continuity of the normal component of

particle velocity at an interface between media having different sound speeds and densities.

The program utilizes concepts developed by earlier authors. The use of the IFD method to solve the parabolic equation in underwater acoustics was developed by Lee and Papadakis (1979). The mathematical treatment of horizontal and sloping interfaces was developed by McDaniel and Lee (1982) and Lee and McDaniel (1983). And finally, the program utilizes some design features of an earlier computer program developed by Lee and Botseas (1982).

## II. PARABOLIC EQUATION

### A. INTRODUCTION

The parabolic equation is an approximation to the elliptical wave equation. The derivation of the parabolic equation begins with the reduced wave equation (Helmholtz equation) in the form

$$\nabla^2 p + k^2 = 0 \quad 2.1$$

or

$$\nabla^2 p + k_0^2 n^2 p = 0 \quad 2.2$$

where

$k$  = wave number ( $= w/c$ )

$k_0$  = reference wave number ( $= w/c_0$ )

$n$  = index of refraction ( $= c_0/c$ )

$p$  = time independent factor of complex pressure

$c$  = sound speed

$c_0$  = reference sound speed

$w$  = angular source frequency ( $= 2\pi f$ )

For the case of cylindrical symmetry (2.2) becomes

$$p_{rr} + (1/r) p_r + p_{zz} + k_0^2 n^2 p = 0 \quad 2.3$$

It is then assumed that  $p$  is of the form

$$p = u(r, z) S(r)$$

where  $u$  is a function of both range and depth and  $S$  is a function of range only. Substitution of (2.4) into (2.3) and separation of variables shows that  $S(r)$  must satisfy

Bessel's equation of zero-order. For  $\exp(-i\omega t)$  time dependence and outgoing waves, the solution is the zeroth-order Hankel function of the first kind,

$$S(r) = H_0^{(1)}(k_0 r).$$

Further,  $u(r, z)$  must satisfy

$$u_{rr} + u_{zz} + \left(-\frac{1}{r} + \frac{2}{S} S_r\right) u_r + k_0^2(n^2 - 1) u = 0. \quad 2.5$$

With the help of the far-field asymptotic approximation for the Hankel function, (2.5) can be reduced to

$$u_{rr} + u_{zz} + 2ik_0 u_r + k_0^2(n^2 - 1) u = 0. \quad 2.6$$

We now assume that  $u$  varies slowly with respect to range,

$$|u_{rr}| \ll |2k_0 u_r|. \quad 2.7$$

combining (2.6) and (2.7) results in

$$u_{zz} + 2ik_0 u_r + k_0^2(n^2 - 1) u = 0. \quad 2.8$$

Rearranging (2.8) results in the parabolic equation in the form

$$u_r = a(k_0, r, z) u + b(k_0, r, z) u_{zz} \quad 2.9$$

where

$$a(k_0, r, z) = (ik_0/2) [n^2(r, z) - 1]$$

$$b(k_0, r, z) = 1/2k_0.$$

The assumption (2.7), fundamental to the parabolic equation method, is equivalent to neglecting back-scatter.

## B. SPLIT-STEP FAST FOURIER TRANSFORM SOLUTION

### 1. Description

For the first few years after its introduction into the acoustical community the parabolic equation was solved

exclusively with the help of the split-step fast Fourier transform (SSFFT) method developed by Tappert and Hardin (Jensen and Krol, 1975). In this method,  $u_{zz}$  in (2.8) is represented by the inverse transform of its Fourier transform. The SSFFT method requires periodic boundary conditions in  $z$  because of the finite Fourier transform. This is handled by introducing an artificial, horizontal, pressure release bottom below the physical bottom. The SSFFT method is unconditionally stable (Brock, 1978).

The SSFFT method has been implemented by Jensen and Krol and by Brock. Detailed descriptions can be found in publications of Jensen and Krol (1975) and Brock (1978).

## 2. Interface Treatment

Errors introduced by the SSFFT method are proportional to the range step and to  $n_{zz}$  where  $n$  is the index of refraction (Jensen and Krol, 1975). Because the index of refraction has a large change across the water-sediment interface  $n_{zz}$  will be large and thus the error will be large. To reduce this error, a very small horizontal range step must be used. However, this results in very long computer execution time. The problem of a discontinuity in sound speed at the water-sediment interface and the resultant difficulties in solving shallow water propagation problems using the SSFFT method are addressed in Jensen and Krol (1975).

Another more serious problem with the SSFFT method is that it neglects any density difference between the water and the sediment. A density difference can be important in that it influences the reflection coefficient. The problem becomes more significant as the density difference becomes larger.

In summary, the discontinuities in sound speed and in density at the water-sediment interface cause problems for the SSFFT method. The SSFFT method is therefore intrinsically better suited for deep water propagation environments for which the water-sediment interface is an unimportant feature.

#### C. IMPLICIT FINITE-DIFFERENCE SOLUTION METHOD

In 1979 Lee and Papadakis introduced the Crank-Nicolson implicit finite-difference method to solve the parabolic equation for underwater acoustic propagation. The Crank-Nicolson method uses a second-order central difference formula to approximate  $u_{zz}$  in (2.9) and casts the problem in the form of a tridiagonal matrix system. A representative row in the matrix system (the  $m^{\text{th}}$  row) is

$$\begin{aligned}
 & \left( -\frac{1}{2} \frac{k}{h^2} b_m^{n+1}, 1 - \frac{1}{2} k a_m^{n+1} + \frac{k}{h^2} b_m^{n+1}, -\frac{1}{2} \frac{k}{h^2} b_m^{n+1} \right) \begin{bmatrix} u_{m-1}^{n+1} \\ u_m^{n+1} \\ u_{m+1}^{n+1} \end{bmatrix} \\
 & = \left( \frac{1}{2} \frac{k}{h^2} b_m^n, 1 + \frac{1}{2} k a_m^n - \frac{k}{h^2} b_m^n, \frac{1}{2} \frac{k}{h^2} b_m^n \right) \begin{bmatrix} u_{m-1}^n \\ u_m^n \\ u_{m+1}^n \end{bmatrix}
 \end{aligned} \tag{2.10}$$

where

$k$  = horizontal range increment

$h$  = vertical depth increment

Superscripts are used to indicate range indices and subscripts are used to indicate depth indices. In (2.10) the field is known at range index  $n$  and is to be solved at range index  $n + 1$ . Therefore, the right hand side of (2.10) reduces to a single, known value and the solution field is advanced from range index  $n$  to range index  $n + 1$  by solving the tridiagonal system of equations.

The IFD scheme is consistent, unconditionally stable and it converges to the theoretical solution as the range and depth increments tend to zero (Lee et al., 1981). An advantage of selecting an implicit scheme over an explicit scheme is that an explicit scheme is only conditionally stable (Lee and Papadakis, 1979). Another advantage of the implicit scheme is smaller errors. More detailed



information addressing both implicit and explicit solutions of parabolic equations can be found in Gerald (1980).

The first IFD scheme handled discontinuities in the speed of sound profile but did not consider the effects of density discontinuities. It therefore did not correctly treat the interface between media having different densities.

#### D. IMPLICIT FINITE-DIFFERENCE METHOD: TREATMENT OF A HORIZONTAL INTERFACE

In 1982 McDaniel and Lee introduced a scheme for incorporating a horizontal interface into the IFD method. The interface separates two media with different sound speeds and densities (Figure 1).

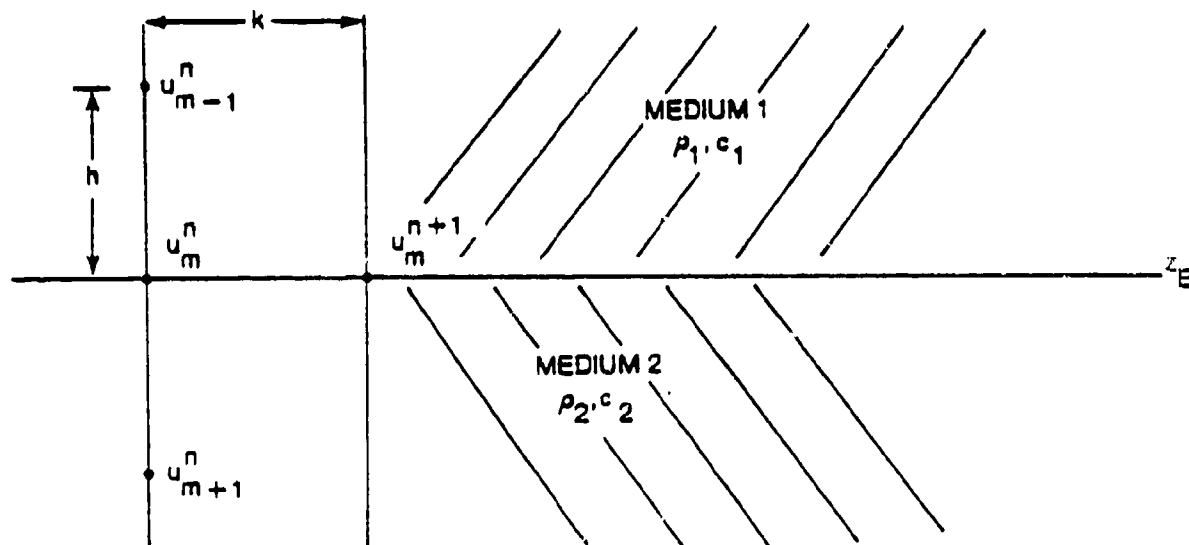


Figure 1. IFD Treatment of a Horizontal Interface

The scheme preserves continuity of pressure and continuity of the normal component of particle velocity across the interface and does not affect the stability of the IFD method.

The interface equation in the tridiagonal matrix system that results from incorporating continuity of pressure and continuity of the normal component of particle velocity is (McDaniel and Lee, 1982)

$$\begin{aligned}
 & \left( -\frac{k}{h^2} p_m^{n+1}, 1 - \frac{1}{2} k p_m^{n+1} Q_m^{n+1} \right. \\
 & \quad \left. + \frac{k}{h^2} p_m^{n+1} \left( 1 + \frac{\rho_1}{\rho_2} \right), -\frac{k}{h^2} p_m^{n+1} \frac{\rho_1}{\rho_2} \right) \begin{bmatrix} u_{m-1}^{n+1} \\ u_m^{n+1} \\ u_{m+1}^{n+1} \end{bmatrix} \\
 & = \left( \frac{k}{h^2} p_m^n, 1 + \frac{1}{2} k p_m^n Q_m^n \right. \\
 & \quad \left. - \frac{k}{h^2} p_m^n \left( 1 + \frac{\rho_1}{\rho_2} \right), \frac{k}{h^2} p_m^n \frac{\rho_1}{\rho_2} \right) \begin{bmatrix} u_{m-1}^n \\ u_m^n \\ u_{m+1}^n \end{bmatrix} \quad 2.11
 \end{aligned}$$

where

$$P = \begin{bmatrix} 1 \\ - \\ b_1 \end{bmatrix} + \frac{\rho_1}{\rho_2} \begin{bmatrix} 1 \\ - \\ b_2 \end{bmatrix}^{-1}$$

$$Q = \begin{bmatrix} a_1 \\ - \\ b_1 \end{bmatrix} + \frac{\rho_1}{\rho_2} \begin{bmatrix} a_2 \\ - \\ b_2 \end{bmatrix}$$

$\rho_1$  = density in layer 1 (water)

$\rho_2$  = density in layer 2 (sediment)

a and b are defined in (2.9)

Incorporating the horizontal interface into the IFD method requires inserting (2.10) for the row in the tridiagonal matrix system that corresponds to the interface.

The error in the solution is

$$O(k^3 + kh)$$

on the interface and

$$O(k^3 + kh^2)$$

in a continuous medium (McDaniel and Lee, 1982).

#### E. IMPLICIT FINITE-DIFFERENCE METHOD: TREATMENT OF A SLOPING INTERFACE

In 1983, Lee and McDaniel extended their treatment of an interface between two media to include the case of a sloping interface. As for the case of a horizontal interface, the treatment of a sloping interface preserves continuity of pressure and continuity of the normal component of particle velocity at the interface between media having different densities and sound speeds.

The problem of a sloping interface is separated into two cases: downslope, and upslope. Each case requires inserting two new rows into the IFD tridiagonal matrix system. One new row is required at the level corresponding to the interface at the range where the solution is known and the second new row is required at the level corresponding to the

interface at the range at which the solution is to be solved. Therefore, four new equations are required to cover both the downslope and upslope cases. The four sloping interface equations are derived and shown in Lee and McDaniel (1983). The equations are somewhat involved but they are of the same tridiagonal form as the original IFD matrix equations. The error for points on or adjacent to a sloping interface is (Lee and McDaniel, 1983)

$$O(k^3 + kh).$$

### III. COMPUTER IMPLEMENTATION

#### A. INTRODUCTION

An IFD solution program that implements (2.10), (2.11) and the four sloping interface equations has been developed to solve underwater propagation problems. The program is written in FORTRAN using single precision, complex arithmetic and has been installed on the Naval Postgraduate School's IBM-3033 digital computer. Appendix A contains a program listing.

The solution program consists of one main program and 20 subroutines. A modular program construction was selected for flexibility and clarity.

Within each routine a structured programming approach is utilized. The structured program format, coupled with generous commenting, makes the program relatively easy to trace through.

As presently installed on the NPS computer the solution program is run interactively. Appendix B contains details.

#### B. GENERAL CHARACTERISTICS

The solution program handles the following environmental conditions: range independent sound speed profile in the water column, range dependent bottom profile and iso-speed, iso-density sedimentary bottom layer. The program utilizes

a Gaussian starting field and an artificial pressure release surface in the sediment at a user-specified depth. (An artificial pressure release surface is not required for the IFD solution method; however, such a surface permits efficient solution for the pressure field when it is known to tend to zero at great depths in the bottom.)

Attenuation in the water and sediment is introduced using complex indices of refraction. Artificially strong attenuation is applied in the lower portion of the sediment layer to enhance attenuation of the field above the artificial pressure release surface.

A user-specified bottom profile is input as a series of linear bottom segments. The range step along a horizontal bottom segment is set to a user-specified value. The range step along a sloping bottom segment is automatically set by the program so that the sloping bottom intersects the next vertical grid point. Bottom modifications are required in certain situations to meet the requirements that the range step not be too large and that the interface must pass through a grid point at every range at which the pressure field is solved. For a very gently sloping bottom, if the calculated range step exceeds a user-specified value then the program will automatically model the bottom as a series of level and sloping sections. For these cases, the difference between the modified bottom and the user-specified bottom is always less than or equal to one-half

the vertical grid increment. The user is informed if the bottom is modified.

It is foreseen that future enhancements will increase the program's generality. In particular, changes to allow range dependent sound speed profiles, sound speed profiles in the sediment and a user-specified starting field should be relatively simple. The modular construction of the program facilitates these types of changes.

#### C. MAIN PROGRAM IFD

IFD is the main program. It controls program execution and calls subroutines as appropriate.

The first executable statement in IFD calls subroutine ERRSET, a system subroutine peculiar to the NPS computer that correctly sets a variable value to zero when an underflow condition exists. Most computer systems do this automatically; however, depending on the particular system a call similar to ERRSET may be required.

IFD then calls subroutine READ to read input data, subroutine SVPW to calculate the sound speed at grid points in the water column, subroutine INITAL to initialize constants and variables, and then subroutine MATCON to calculate matrix constants. Subroutine SFIELD is then called to calculate the Gaussian starting field, followed by subroutines WRITE1 and PRINT1 which write and print output data. In the context of this program, "write" refers to

writing unformatted data into a file to be used by the plotting routine and "print" refers to writing formatted data into a file which can be sent directly to the printer.

IFD then calls subroutine NEWSEG which is the beginning of a loop that is called every time a new linear bottom segment is reached. NEWSEG calculates variables that characterize a new bottom segment. The next call is to subroutine NEWMAT which calculates matrix elements for the new bottom segment and advances the solution field one range step. IFD then enters a loop that advances the solution one range step for every pass through the loop. Inside the loop the range markers are advanced and the solution is advanced one step for the downslope, level, upslope, modified bottom downslope or modified bottom upslope situation as appropriate. In addition, the artificial attenuation mentioned earlier is applied by calling ATTENU and calls are made to WRITE2 or PRINT2 as required. Finally the range is checked to see if it has advanced to the maximum range specified for the problem. If it has, then IFD calls subroutine END which passes appropriate messages to the terminal and stops program execution.

#### D. SUBROUTINES

##### 1. Subroutine READ

Subroutine READ is called by IFD to read input data from unit number NIU = 51. Input data are read in free



format and data are transferred back to main program IFD via common blocks. READ contains error checks for (1) input data insufficient and (2) the final depth in the sound speed profile unequal to the maximum depth in the water column. If either of these error conditions exists, READ issues an appropriate error message to the terminal and stops execution.

## 2. Subroutine SVPW

Subroutine SVPW calculates the vertical grid spacing used in the water and sediment. It also calculates the speed of sound at each of the grid points in the water column. Linear interpolation is used to calculate the sound speed at grid points between points on the user-specified sound speed profile.

## 3. Subroutine INITAL

Subroutine INITAL initializes constants and variables. If the user inputs 0.0 for the value of the reference sound speed then INITAL sets the reference sound speed  $c_0$  to the sound speed averaged over the deepest water column. If the user inputs 0.0 for the value of the maximum range step then INITAL sets the maximum range step to the reference wavelength,

$$DRMAX = XLAMDA \quad .$$

Setting the maximum range step to the reference wavelength is somewhat arbitrary; however, until the actual limit on the range step is better understood it serves as a rough

rule of thumb. Finally, if the user inputs 0.0 for the value of the range step along a horizontal interface then INITIAL sets the range step to half of the reference wavelength,

$$DRLVL = 0.5 * XLAMDA.$$

The default range step along a horizontal interface is half the default maximum range step.

#### 4. Subroutine MATCON

Subroutine MATCON calculates constants needed to compute tridiagonal matrix elements. Most of the constants computed in MATCON have no direct physical significance but contribute to computational efficiency. Attenuation in both the water and sediment is calculated with the help of a complex index of refraction  $n$ ,

$$n = \begin{bmatrix} c_0 \\ c_j \end{bmatrix} \left( 1 + i \frac{BETA}{54.575054} \right)$$

or

$$n^2 = \begin{bmatrix} c_0 \\ c_j \end{bmatrix}^2 + i \begin{bmatrix} c_0 \\ c_j \end{bmatrix}^2 \frac{BETA}{27.287527}$$

where

BETA = attenuation (dB/wavelength)

$c_0$  = reference sound speed (m/s)

$c_j$  = sound speed (m/s) at point  $j$

54.575054 = conversion factor used in converting  
db/wavelength to nepers/meter.

### 5. Subroutine SFIELD

Subroutine SFIELD calculates the Gaussian starting field at range  $r = 0$ . This subroutine is identical with that of Lee and Botseas (1982); both yield the starting field suggested by Brock (1978),

$$U(I) = \text{CMPLX} (PR, 0.0)$$

where

$$PR = GA \left[ e^{-\left[ \frac{ZM-ZS}{GW} \right]^2} - e^{-\left[ \frac{-ZM-ZS}{GW} \right]^2} \right]$$

ZM = depth (m) of grid point

ZS = source depth (m)

GW = Gaussian width (m) ( $= 2/FK$ )

FK = reference wave number (1/m) ( $= 2\pi f/c_0$ )

GA = Gaussian amplitude [ $= (2/FK)^{1/2}/GW$ ]

### 6. Subroutine WRITE1

Subroutine WRITE1 outputs data to a file that is used by the plotting routine. This output file corresponds to unit file number NOU = 52.

### 7. Subroutine PRINT1

Subroutine PRINT1 outputs formatted data to a file that can be sent to the printer. The output file corresponds to unit file number NPOUT = 55.

#### 8. Subroutine NEWSEG

Subroutine NEWSEG is called at the start of each new linear bottom segment. NEWSEG computes and initializes variables that depend on characteristics of the segment. One of the variables initialized is ISLOPE which is a slope flag having value 1 if the bottom slopes down, 2 if the bottom is horizontal, 3 if the bottom slopes up, 4 if the bottom slopes down but must be modified because the slope is very small, or 5 if the bottom slopes up but must be modified because the slope is very small. NEWSEG also issues error or warning messages as appropriate.

#### 9. Subroutine NEWMAT

Subroutine NEWMAT calculates matrix elements for the X and Y matrices. The Y matrix corresponds to the range at which the solution field is known and the X matrix corresponds to the range at which the solution field is to be found. The Y matrix is multiplied by the known solution field to obtain the right-hand side column vector needed to solve the tridiagonal system.

NEWMAT sets up the tridiagonal matrix system for the new bottom segment and then calls TRIDG to solve the system at the first range step. It then calls ATTENU to apply artificial attenuation, calls WRITE2 or PRINT2 as required, and finally updates the interface pointer that indicates the index of the grid point at the water-sediment interface.

#### 10. Subroutine WRITE2

Subroutine WRITE2 is basically a continuation of subroutine WRITE1. It outputs data to a file corresponding to unit file number NOU = 52. This is the file that is used by the plotting routine. At range intervals specified by the user, WRITE2 outputs range, depth, and the value of  $u(r,z)$ .

#### 11. Subroutine PRINT2

Subroutine PRINT2 is basically a continuation of subroutine PRINT1. It outputs formatted data to a file corresponding to unit file number NPOUT = 55. This file can be sent directly to the printer. At range and depth intervals specified by the user PRINT2 outputs tabular values of transmission loss and  $u(r,z)$ .

#### 12. Subroutine TRIDG

Subroutine TRIDG solves a linear tridiagonal matrix system. TRIDG is a modified version of subroutine TRID as listed in Gerald (1980). The major modifications to subroutine TRID involved introducing arrays CTWO and CR to preserve the original matrix element values and to make the routine more efficient. Introducing the two new arrays requires more storage space but results in a substantial savings in execution time, particularly for the case of a horizontal interface.

### 13. Subroutine TRIDL

Subroutine TRIDL is a modified version of subroutine TRIDG. TRIDL differs from TRIDG in that it does not compute arrays CTWO and CR but rather uses the array values calculated in TRIDG.

### 14. Subroutine DOWN

Subroutine DOWN updates the tridiagonal matrix and calls subroutine RHS to update the right-hand side for the case of a downward sloping interface. DOWN then calls subroutine TRIDG to solve the tridiagonal system of equations and finally updates the interface pointer.

### 15. Subroutine UP

Subroutine UP performs exactly the same tasks as subroutine DOWN, but for the case of an upward sloping interface. Subroutine TRIDG is again called to solve the system.

### 16. Subroutine LEVEL

Subroutine LEVEL is called to advance the solution for the case of a horizontal interface. For this case the tridiagonal matrix elements at the advanced range need not be changed from the previous calculation. Therefore, LEVEL need only update the right-hand side by calling RHS and then solve the system by calling TRIDL.

### 17. Subroutine RHS

Subroutine RHS computes the right-hand side of the tridiagonal system by multiplying tridiagonal matrix Y by

the known solution field U(I). The resultant right-hand side column vector is stored in C(I,4).

18. Subroutine SSLOPE

Subroutine SSLOPE is called to advance the solution in the case where the bottom has been modified. SSLOPE determines which of three cases a particular section falls into: a level section following a level section, a level section following a sloping section, or a sloping section. For the case of a level section following a level section SSLOPE calls LEVEL to advance the solution. For the case of a level section following a sloping section SSLOPE updates appropriate matrix elements, calls RHS and then calls TRIDG to advance the solution. And in the case of a sloping section SSLOPE updates matrix elements and calls either DOWN or UP as appropriate.

19. Subroutine ATTENU

Subroutine ATTENU applies artificial attenuation to the bottom portion of the sediment layer as suggested by Brock (1978). The artificial attenuation matrix ATT(1) is calculated in subroutine NEWMAT.

20. Subroutine END

Subroutine END is called when the solution field has reached the maximum range specified. END sends appropriate messages to the terminal and stops execution. The messages are applicable to the program as installed on the NPS

computer but may not be appropriate for the program if installed on another system.

## E. INPUT DATA

### 1. Input File

The input data must be stored in a file corresponding to unit number NIU as assigned in subroutine READ. In its present form READ sets the input unit number to NIU = 51. If the user prefers to read the data from a different unit (for example, a card reader), then variable NIU in READ should be set equal to the appropriate unit number.

### 2. Input Format

The input data is read in free format. The input card images (or input cards) are arranged as follows:

<u>CARD</u>	<u>CONTENTS</u>
-------------	-----------------

1	FRQ, ZS, ZR, C0, N
---	--------------------

where

FRQ = frequency (Hz)

ZS = source depth (m)

ZR = receiver depth (m)

(program will reset to depth of nearest grid point)

C0 = reference sound speed (m/s)

If C0 = 0.0, C0 is set to the sound speed averaged over the deepest water column.



N = number of vertical grid points

If the user desires that every integer depth value correspond to a grid point then (neglecting dimensions) N should be set to an integer multiple of ZLYR2, the depth of the pressure release surface.

<u>CARD</u>	<u>CONTENTS</u>
-------------	-----------------

2	RMAX, DRLVL, DRMAX, WDR, PDR, PDZ
---	-----------------------------------

where

RMAX = maximum range (m) of solution

DRLVL = range step (m) for marching solution  
along horizontal interface

If DRLVL = 0.0, then DRLVL is set to 1/2  
wavelength.

If DRLVL is greater than DRMAX, then  
DRLVL is set to DRMAX.

DRMAX = maximum allowable range step (m)

If DRMAX = 0.0, then DRMAX is set to 1  
wavelength.

WDR = range increment (m) at which solution is  
written to file used by plotting routine

PDR = range increment (m) at which solution is  
printed

PDZ = depth increment (m) rounded to nearest DZ  
at which solution is printed

<u>CARD</u>	<u>CONTENTS</u>		
3	BR(1)	BZ(1)	} <u>BOTTOM PROFILE</u> Range and depth of water (m). Maximum number of points = 100. Program will reset depths to nearest grid point.
4	BR(2)	BZ(2)	
5	BR(3)	BZ(3)	
.	.	.	
.	.	.	
N	.	.	
N+1	-1	-1	This card marks end of bottom profile.

N+2      ZLYR1, RHO1, BETA1

where

ZLYR1    = maximum water depth (m)

RHO1     = density of water (g/cm<sup>3</sup>)

BETA1    = attenuation in water (dB/meter)

If BETA1 is less than 0.0 then program calculates BETA1 with an empirical formula (Brock, 1978).

N+3	ZSVP(1),	CSVP(1)	} <u>SOUND SPEED PROFILE</u> Depth (m) and sound speed (m/s). ZSVP(1) must equal 0. The last depth must equal ZLYR1.
N+4	ZSVP(2),	CSVP(2)	
.	.	.	
.	.	.	
N+M			

CARD    CONTENTS

N+M+1    ZLYR2, RHO2, BETA2, C2

where

ZLYR2    = depth (m) of pressure release surface at  
          bottom of sediment layer

RHO2     = density ( $\text{g/cm}^3$ ) of sediment

BETA2    = attenuation (dB/wavelength) in sediment

C2       = sound speed (m/s) in sediment

N+M+2    ZABLYR

where

ZABLYR = depth (m) of upper surface of artificial  
          attenuation layer in sediment.

ZABLYR should be about 3/4 of ZLYR2.

F.    PROGRAM OUTPUT

1.    Output Printer File

The program outputs formatted data to a file corresponding to unit number NPOUT which is set to 55. This formatted data file may be sent to the printer if desired. On another system the user may elect to assign NPOUT to the unit number corresponding to the printer and thereby send the formatted data directly to the printer.

2.    Output Plotter File

The program outputs unformatted data to a file that is used by the plotting routine. The unit number for this

file is NOU which is set to 52. The output data in this file are stored as follows:

<u>LINE</u>	<u>CONTENTS</u>
-------------	-----------------

1	RMAX
---	------

where

RMAX = maximum range (m) of solution

2	RA, ZR, U
---	-----------

3	RA, ZR, U
---	-----------

.	.	.	.
---	---	---	---

.	.	.	.
---	---	---	---

where

RA = range (m)

ZR = depth (m)

U = complex u at specified range and depth

### 3. Terminal Output

Certain WRITE statements in the program specify unit number 6. Unit number 6 on the NPS computer for an interactive program corresponds to terminal output. If the program is not run interactively then WRITE statements with unit number 6 may be deleted. Any pertinent information passed to the terminal during an interactive run is also passed to unit number 55.

### G. PLOTTING PROGRAM

Appendix C contains a listing of the IFD plotting program installed on the NPS computer. The filename and

filetype of the program are PLOTIFD FORTRAN. This program was written separately from the IFD program because it was recognized that different computer installations have different plotting facilities. For users with different facilities the program will be a helpful reference.

The program reads data from unit number NOU = 52 which corresponds to a file with filename/filetype IFDOUT PLOTTER. Details concerning using the plotting routine are included in Appendix B.

#### IV. TEST CASES

##### A. HORIZONTAL INTERFACE CASES

The IFD program treats a horizontal interface using the same theoretical approach as the IFD program published by Lee and Botseas (1982). Throughout the remainder of this thesis the Lee and Botseas (1982) program will be called the FINITE-DIFFERENCE program and the program presented in this thesis will be called the IFD program. Two cases were run to confirm that the IFD program is in agreement with the FINITE-DIFFERENCE program for horizontal interfaces.

##### 1. Isospeed Shallow Water

This case, first published by Jensen and Kuperman (1979), considers propagation in a shallow water, isospeed environment. The water depth is 100 meters and the solution field is calculated out to 25 kilometers. The sound speed is 1500 m/s in the water and 1550 m/s in the sediment. Density and attenuation in the sediment are  $1.2 \text{ g/cm}^3$  and 1 dB/wavelength respectively. The source and receiver are both at 50 m and the source frequency is 500 Hz.

Solutions obtained using a normal mode program (SNAP), a split-step fast Fourier transform program (PAREQ) and the FINITE-DIFFERENCE program are shown in Figure 2. SNAP and PAREQ are programs that were developed at SACLANC Centre and are discussed further in Jensen and Kuperman

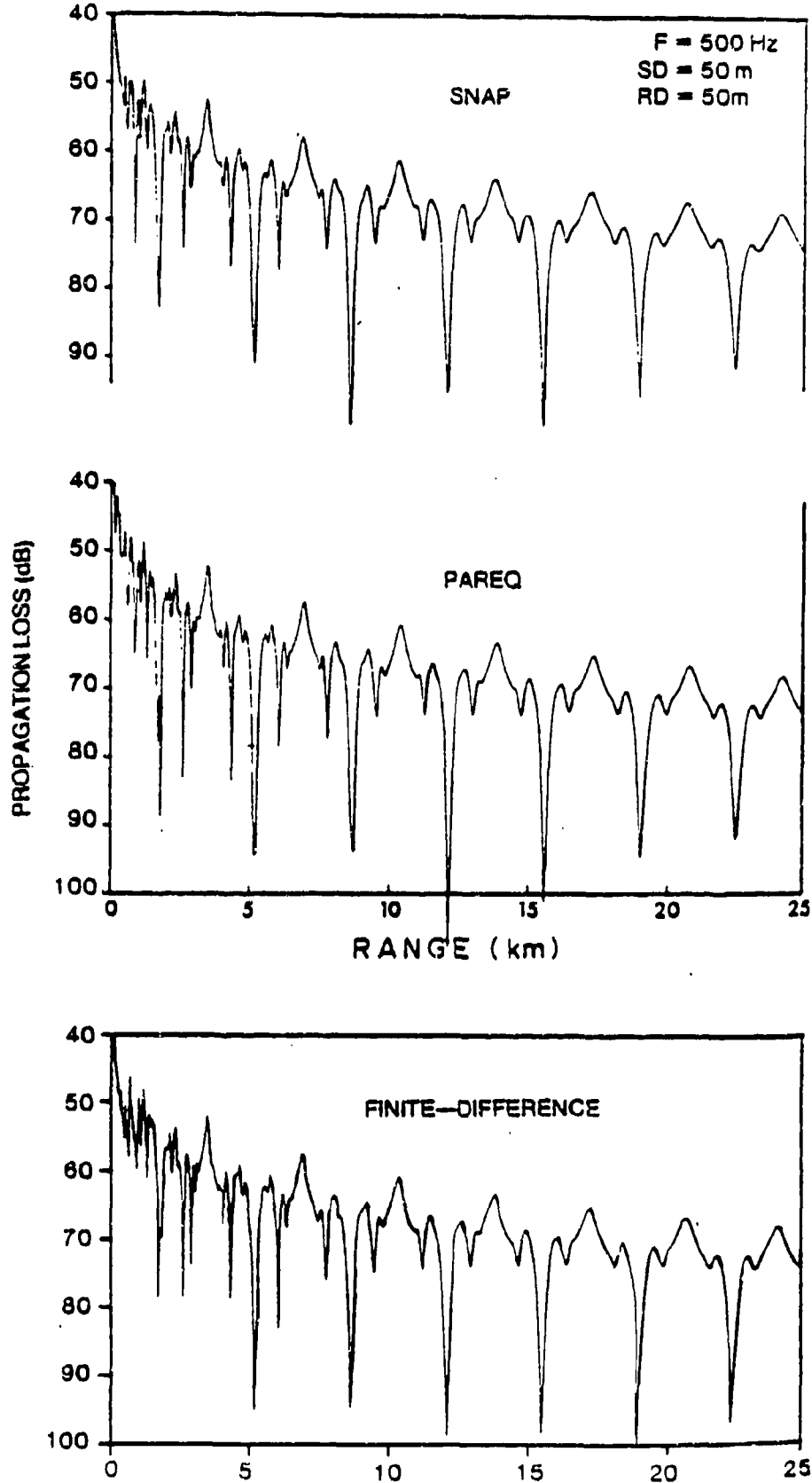


Figure 2. Propagation Loss Versus Range for Shallow Water Case; SNAP, PAREQ and FINITE-DIFFERENCE Results

(1979). The solution obtained using the IFD program is shown in Figure 3. All of the solutions are in excellent agreement.

The input runstream that produced the results shown in Figure 3 for the IFD program is as follows:

<u>Input Runstream</u>					
500	50	50	0	500	
25000	5	5	50	5000	50
0		100			
25000		100			
-1		-1			
100	1.0	-1.0			
0		1500			
100		1500			
250	1.2	1.0	1550		
200					

## 2. Horizontal Interface

This case, called the "horizontal interface problem" in Lee and Botseas (1982), considers propagation in an environment with the sound speed profile shown in Figure 4. Source frequency is 100 Hz, source depth is 30 m and receiver depth is 90 m. The density in the bottom is  $2.1 \text{ g/cm}^3$  and the sound speed in the bottom is 1505 m/s. No attenuation is applied in the water or sediment using complex indices of refraction; however, artificial attenuation is applied in the lower portion of the sediment layer.



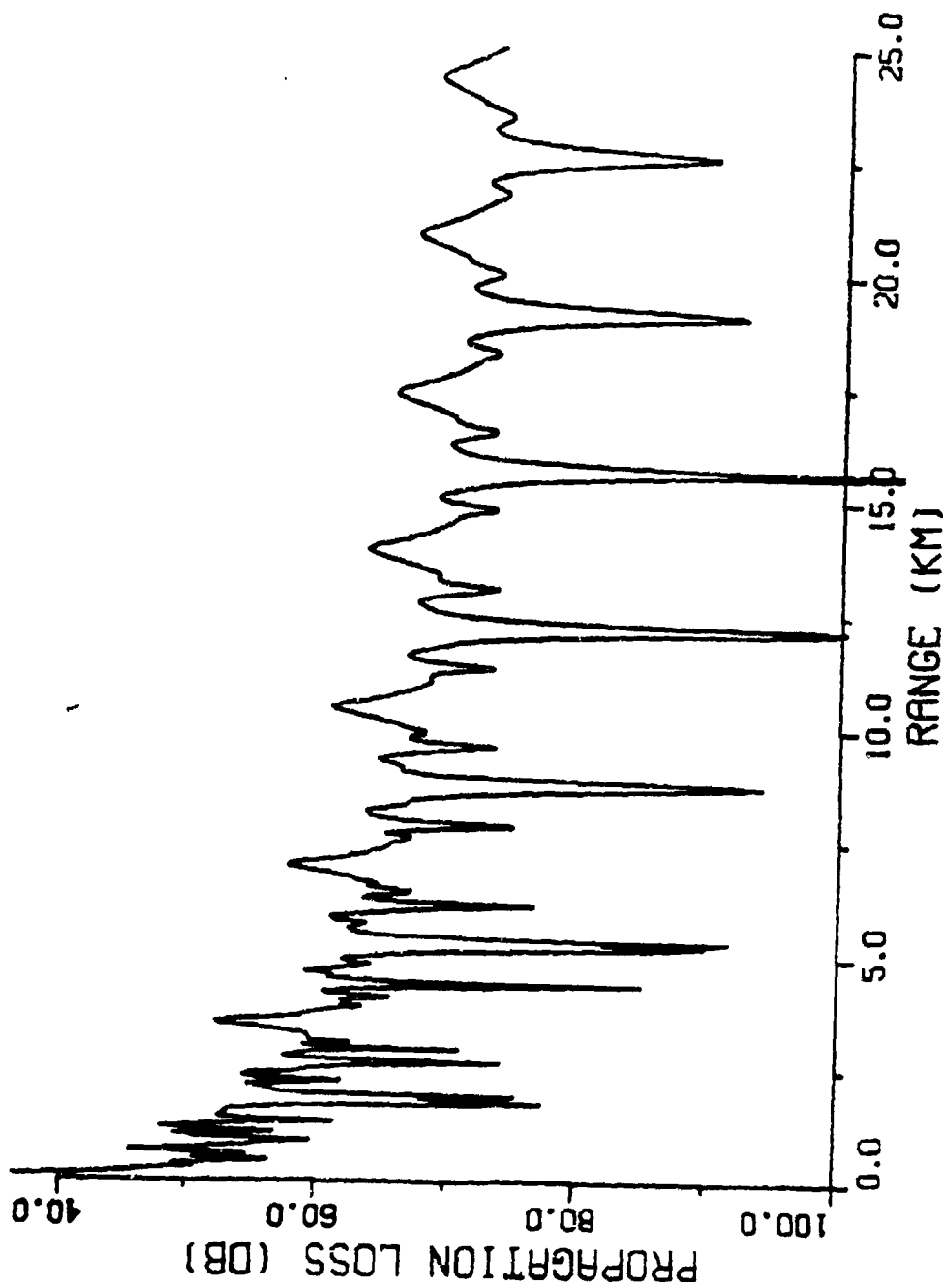


Figure 3. Propagation Loss Versus Range for Shallow Water Case; IFD Results

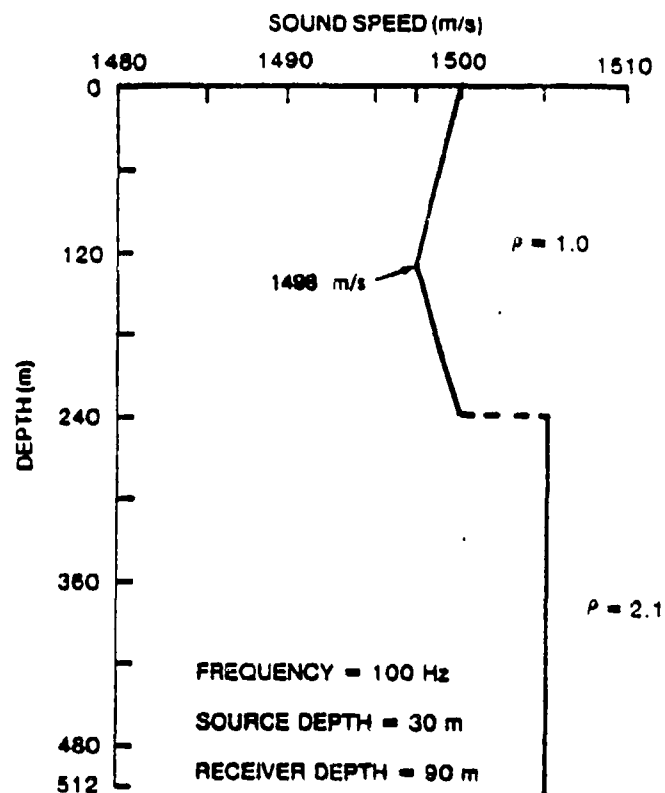


Figure 4. Horizontal Interface Case

The solution obtained using the IFD program is shown in Figure 5. This solution is in excellent agreement with the FINITE-DIFFERENCE solution shown in Lee and Botseas (1982).

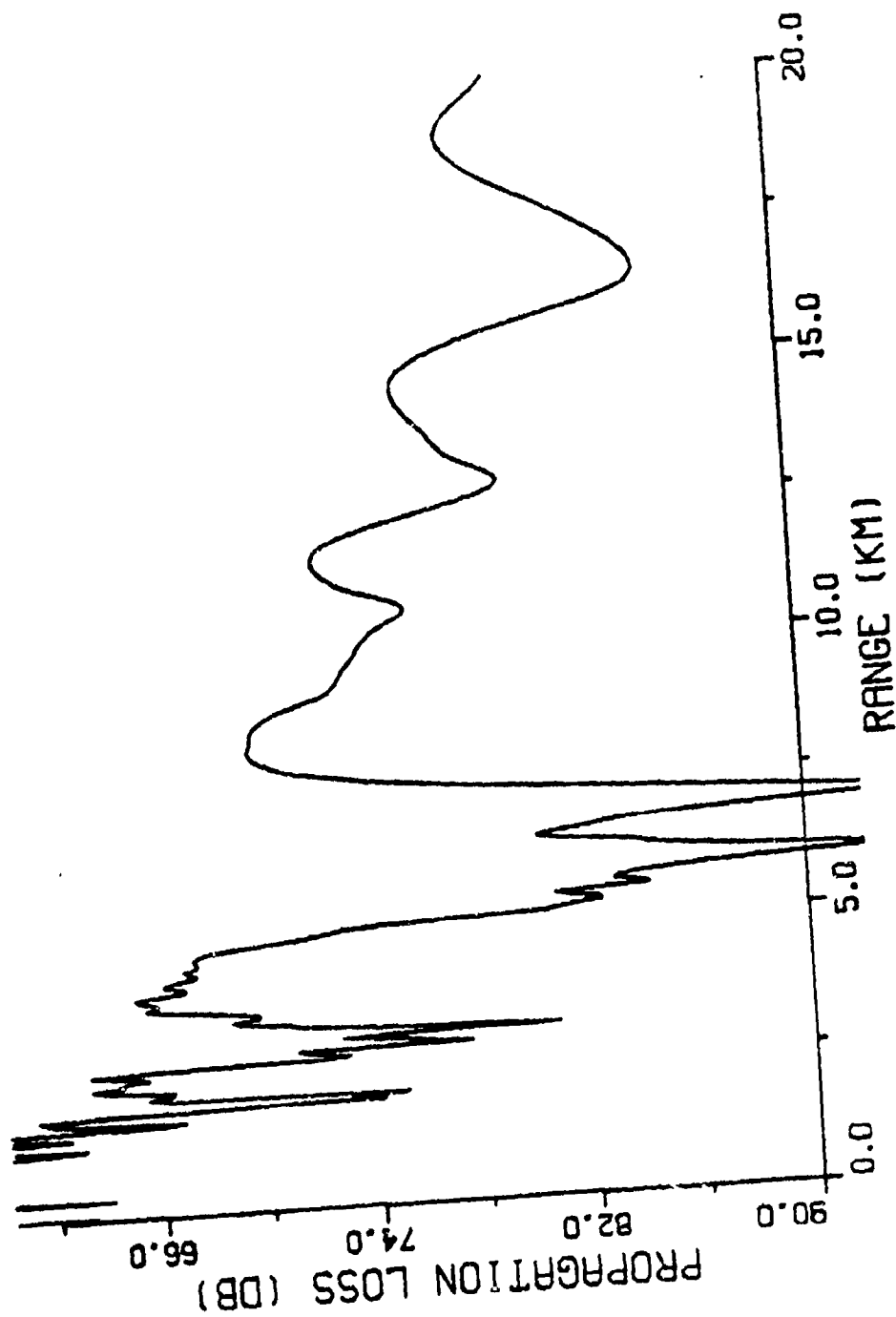


Figure 5. Propagation Loss Versus Range for Horizontal Interface Case; IFD Results

The input runstream for this case is as follows:

<u>Input Runstream</u>					
100	30	90	0	600	
20000	2	2	50	10000	50
0	240				
20000	240				
-1	-1				
240	1.0	0.0			
0	1500				
120	1498				
240	1500				
1200	2.1	0.0	1505		
512					

#### B. RANGE-DEPENDENT CASES

The following range-dependent cases were solved by Jensen and Kuperman using SNAP, the normal mode program, and PAREQ, the SSFFT program (Jensen and Kuperman, 1979). The cases were also solved by Lee and Botseas using the FINITE-DIFFERENCE program (Lee and Botseas, 1982). The FINITE-DIFFERENCE program treats the sloping interface as a "stair step" and uses the interface conditions appropriate for a horizontal interface. The IFD program handles the sloping interface using the interface treatment derived by Lee and McDaniel (1983).

### 1. Deep-to-Shallow Water

This case considers propagation in an environment as depicted in Figure 6. The problem is solved for a bottom with a 8.5 degree upslope and one with a 0.85 degree upslope. Source frequency is 25 Hz, source depth and receiver depth are 25 meters. Sound speed in the water is 1500 m/s. In the sediment, sound speed is 1600 m/s, density is  $1.5 \text{ g/cm}^3$  and attenuation is 0.2 dB/wavelength.

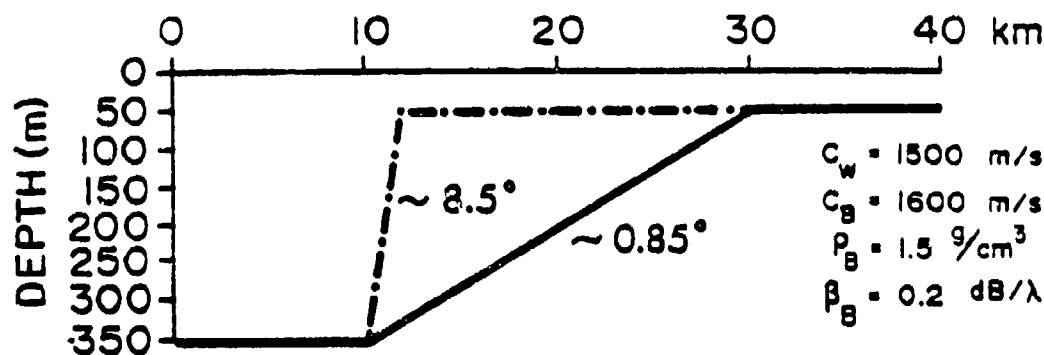


Figure 6. Deep-to-Shallow Water Case

The results for the 8.5 degree upslope case as produced by SNAP, PAREQ, and FINITE-DIFFERENCE are shown in Figure 7. The results as produced by IFD are shown in Figure 8. The difference between the results produced by SNAP and PAREQ is attributed to failure of the "adiabatic" theory underlying the SNAP program (Jensen and Kuperman, 1979). As determined from the input runstream the FINITE-DIFFERENCE results were obtained using 1.0 rather than  $1.5 \text{ g/cm}^3$  for the density in the sediment (Lee and Botseas, 1982).

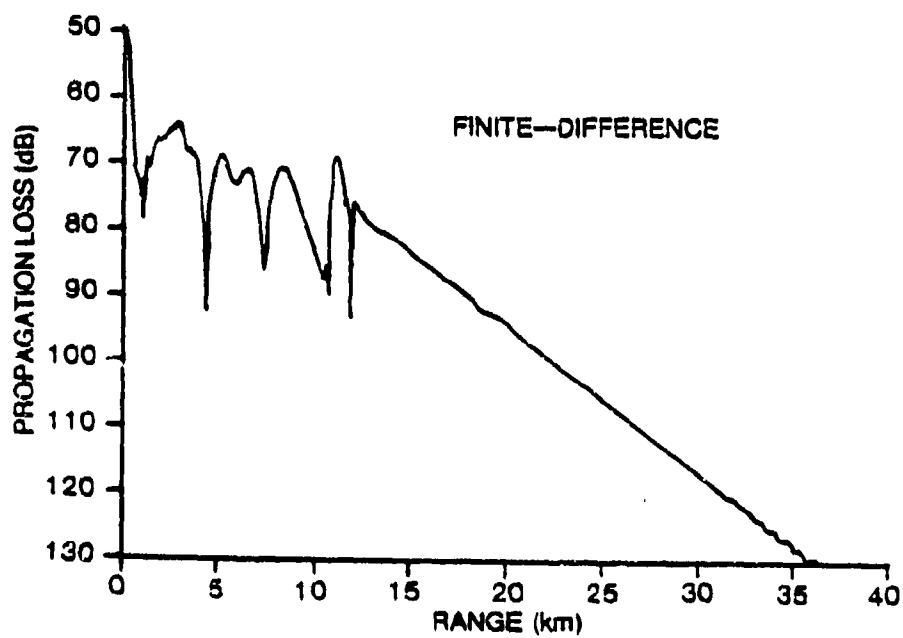
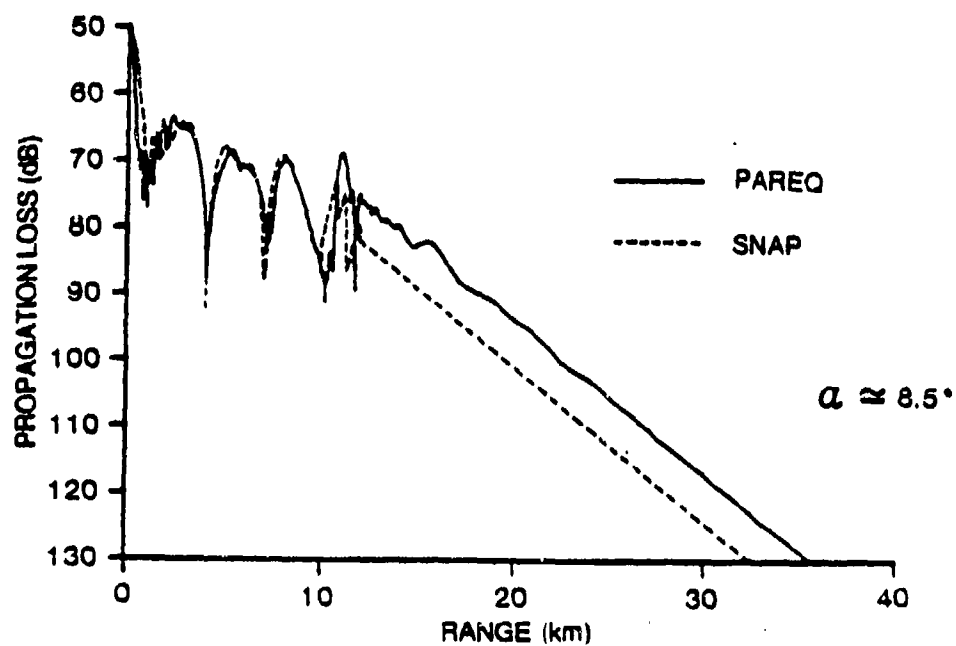


Figure 7. Propagation Loss Versus Range for Deep-to-Shallow Water Case, 8.5 Degree Slope; SNAP, PAREQ and FINITE-DIFFERENCE Results

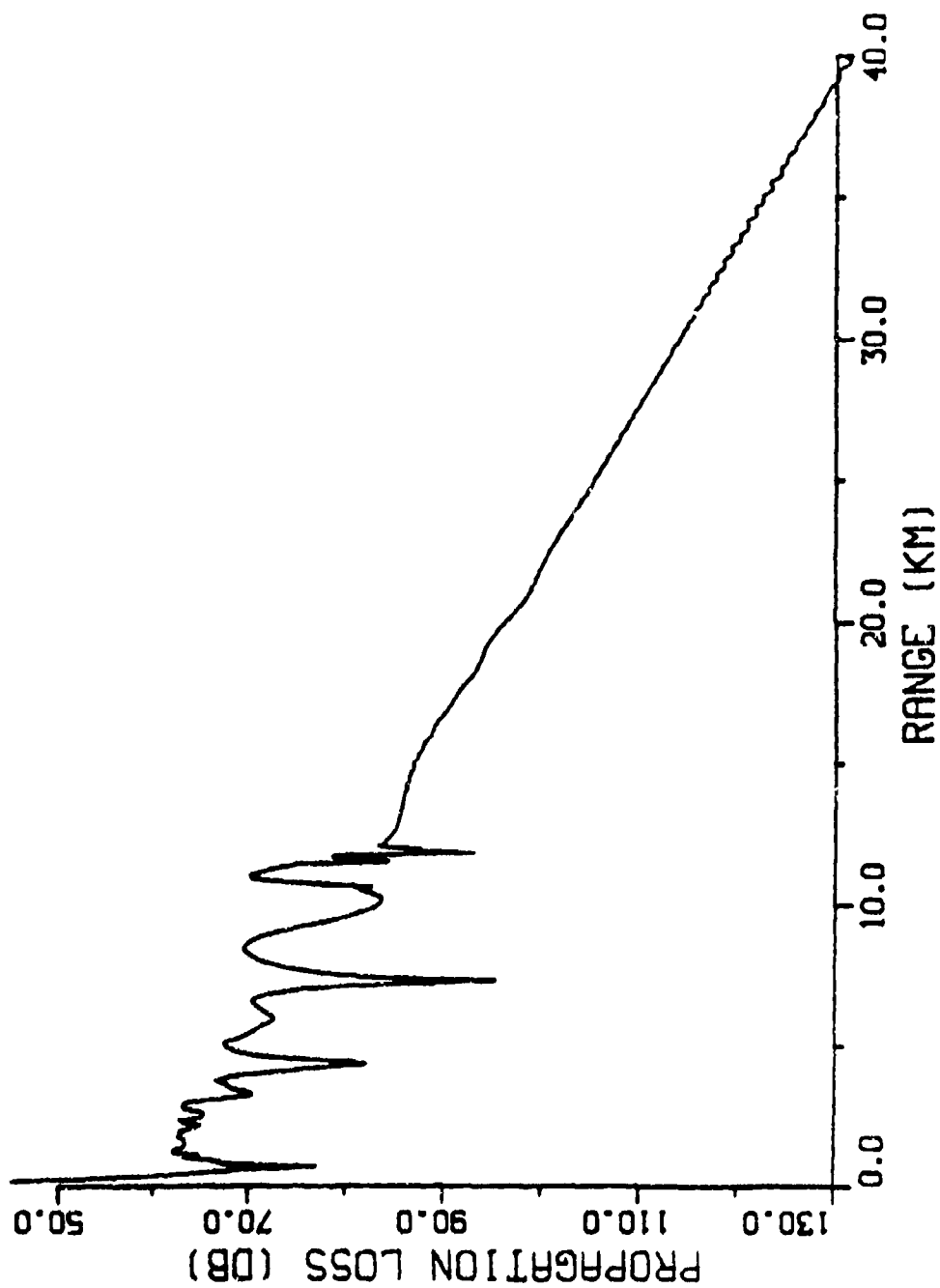


Figure 8. Propagation Loss Versus Range for Deep-to-Shallow Water Case, 8.5 degree Slope; IFD Results

The input runstream for the IFD program that produced the results shown in Figure 8 is as follows:

<u>Input Runstream</u>					
25	25	25	0	1000	
40000	10	0	100	10000	25
0	350				
10000	350				
12000	50				
40000	50				
-1	-1				
350	1.0	-1			
0	1500				
350	1500				
1000	1.5	0.2	1600		
750					

Appendix D contains the printed output produced by the IFD program using the above runstream.

The results for the 0.85 degree upslope case as produced by SNAP and PAREQ are shown in Figure 9. The results produced by IFD are shown in Figure 10.

## 2. Shallow-to-Deep Water

This case considers propagation in the environment depicted in Figure 11. The environment is exactly the same as the deep-to-shallow water environment except that the shallow and deep portions have been reversed and thus the bottom slopes down rather than up.



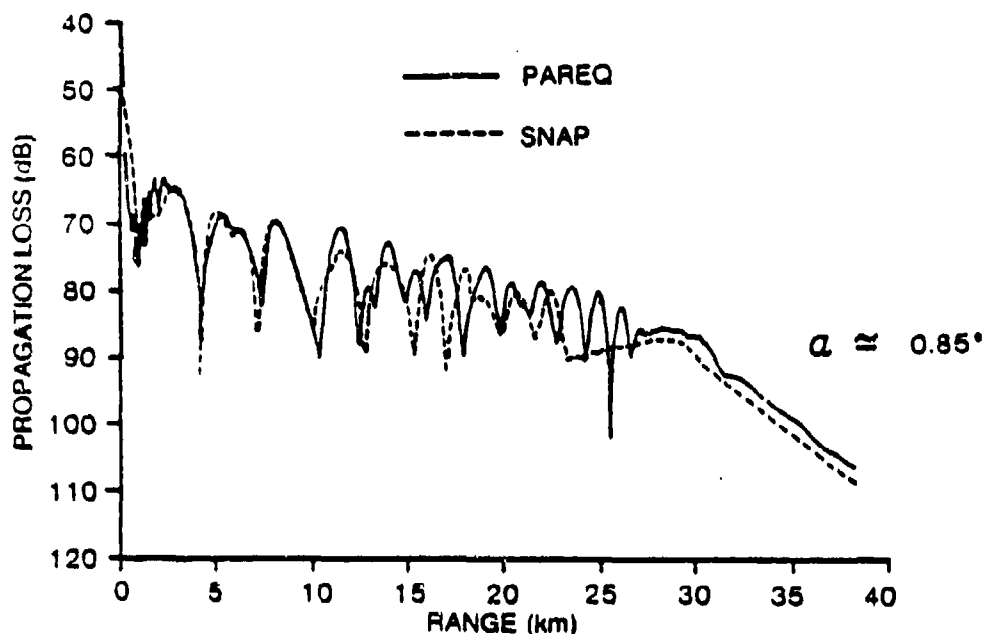


Figure 9. Propagation Loss Versus Range for Deep-to-Shallow Water Case, 0.85 Degree Slope; SNAP and PAREQ Results

The results for the 8.5 degrees downslope case as produced by SNAP and PAREQ are shown in Figure 12. As before, the difference between SNAP and PAREQ is attributed to failure of the SNAP program. The results produced by IFD are shown in Figure 13.

The results for the 0.85 degree downslope case are shown in Figures 14 and 15.

### 3. Comments

Differences between the results obtained using the SNAP and PAREQ programs for the range-dependent cases are discussed in Jensen and Kuperman (1979). The major differences are attributed to the violation of the adiabatic assumption in the SNAP program.

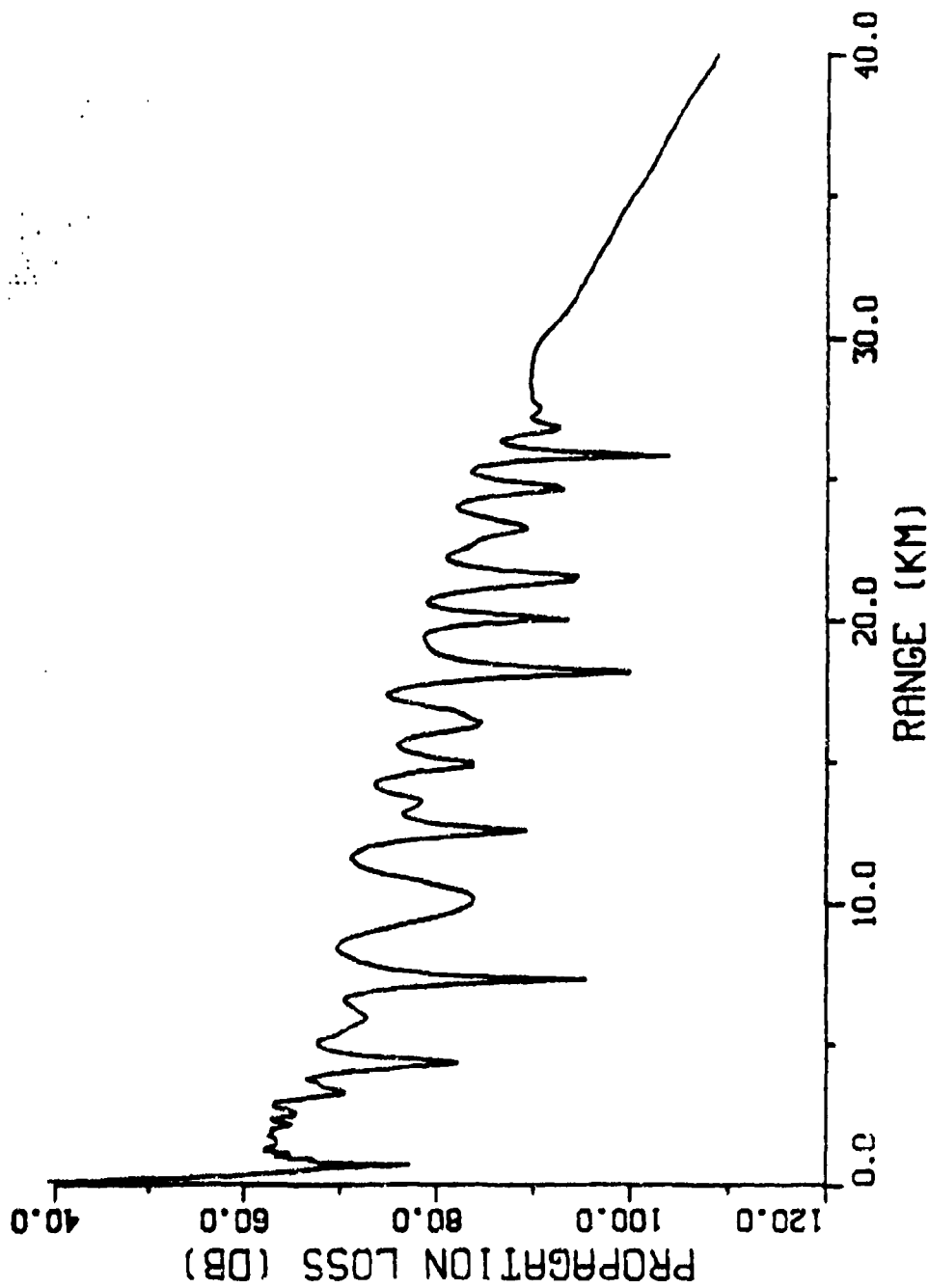


Figure 10. Propagation Loss Versus Range for Deep-to-Shallow Water Case; 0.85 degree Slope; IFD Results

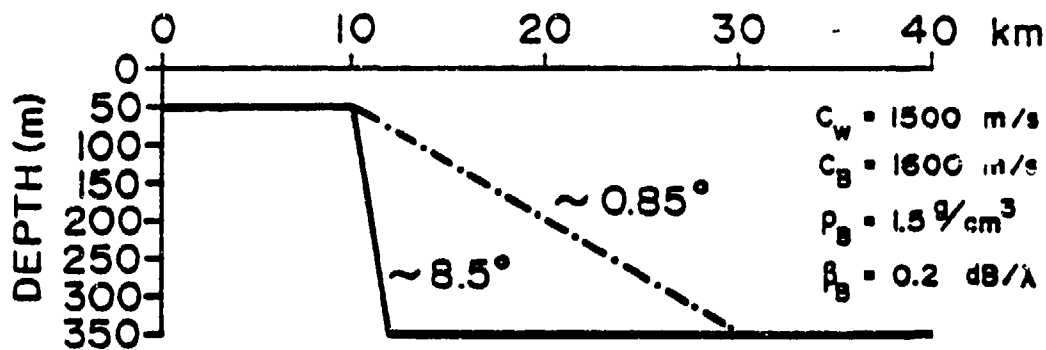


Figure 11. Shallow-to-Deep Water Case

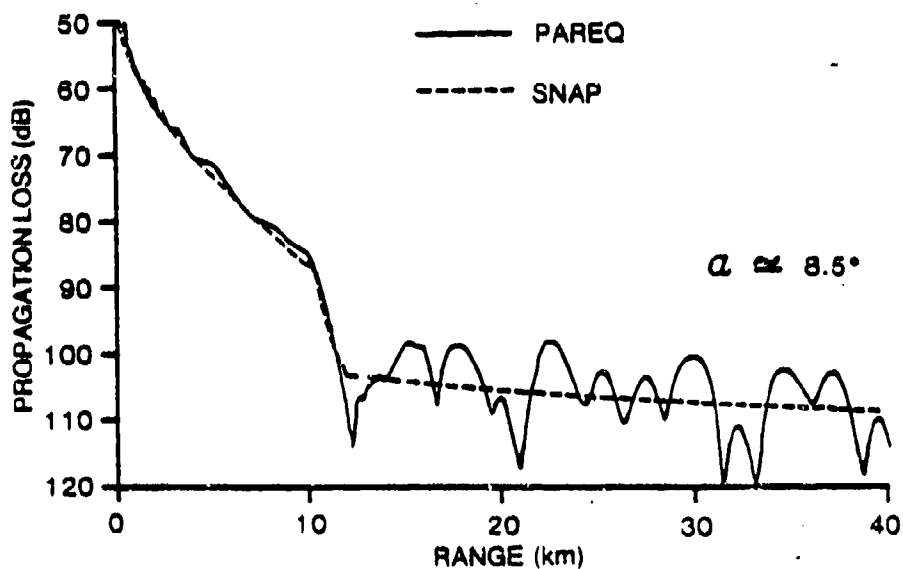


Figure 12. Propagation Loss Versus Range for Shallow-to-Deep Water Case. 8.5 degree Slope; SNAP and PAREQ Results

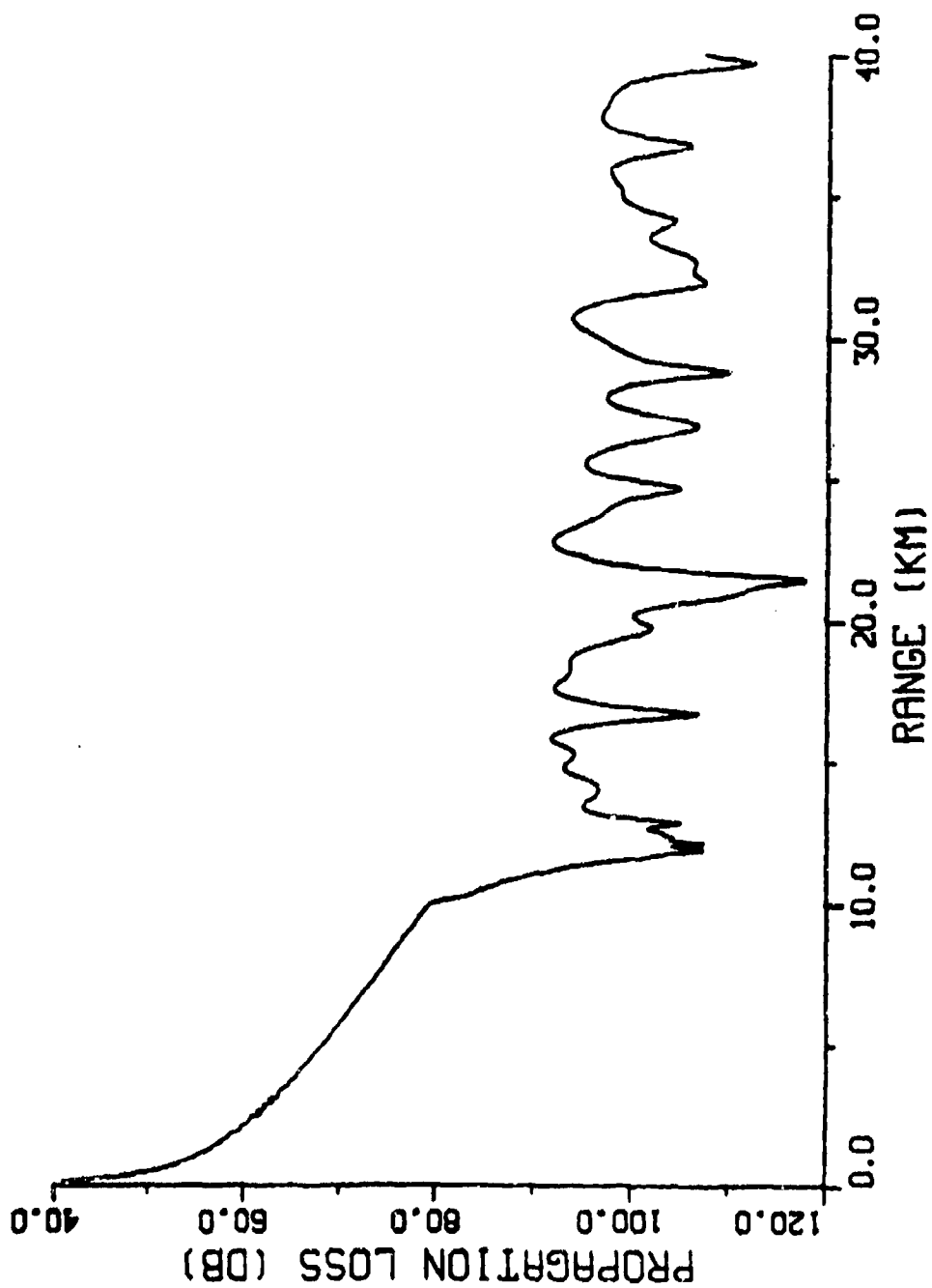


Figure 13. Propagation Loss Versus Range for Shallow-to-Deep Water Case, 8.5 degree Slope; IFD Results

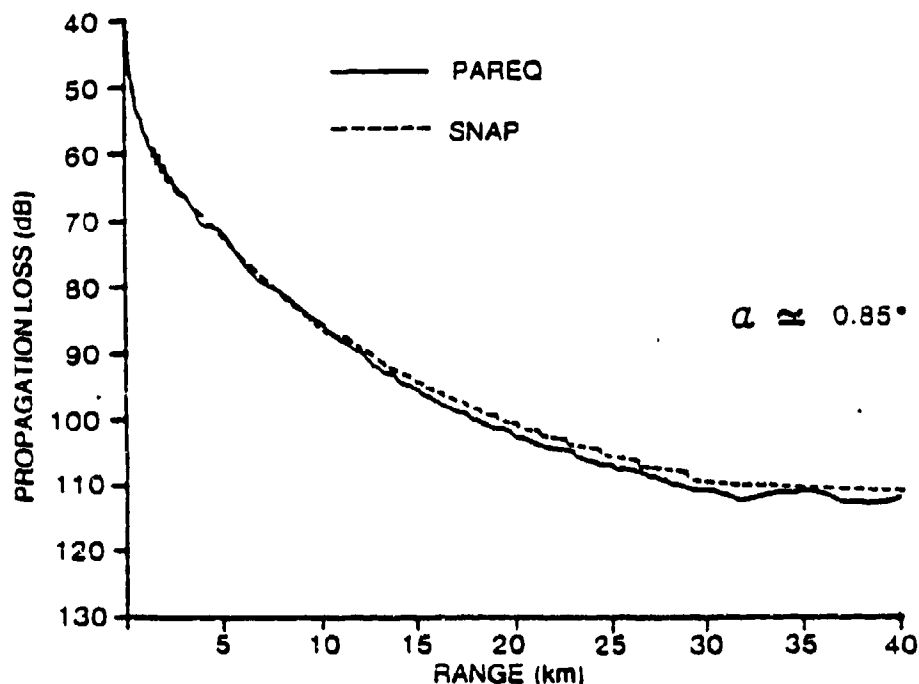


Figure 14. Propagation Loss Versus Range for Shallow-to-Deep Water Case, 0.85 degree Slope; SNAP and PAREQ Results

Figure 16 shows the results produced by IFD for the 8.5 degree, deep-to-shallow water case if 1.0 rather than 1.5 g/cm<sup>3</sup> is used for the density of the sediment. The IFD results obtained using 1.0 g/cm<sup>3</sup> are in very close agreement with the PAREQ results shown in Figure 7. However, when the correct value of 1.5 g/cm<sup>3</sup> is used the slope of the propagation loss curve beyond 15 km is less steep (Figure 8) and the results do not agree as well with the results produced by PAREQ. The observation that the slope of the propagation loss curve becomes less steep when 1.5 g/cm<sup>3</sup> is used is qualitatively consistent because a higher density difference means a higher reflection coefficient which in

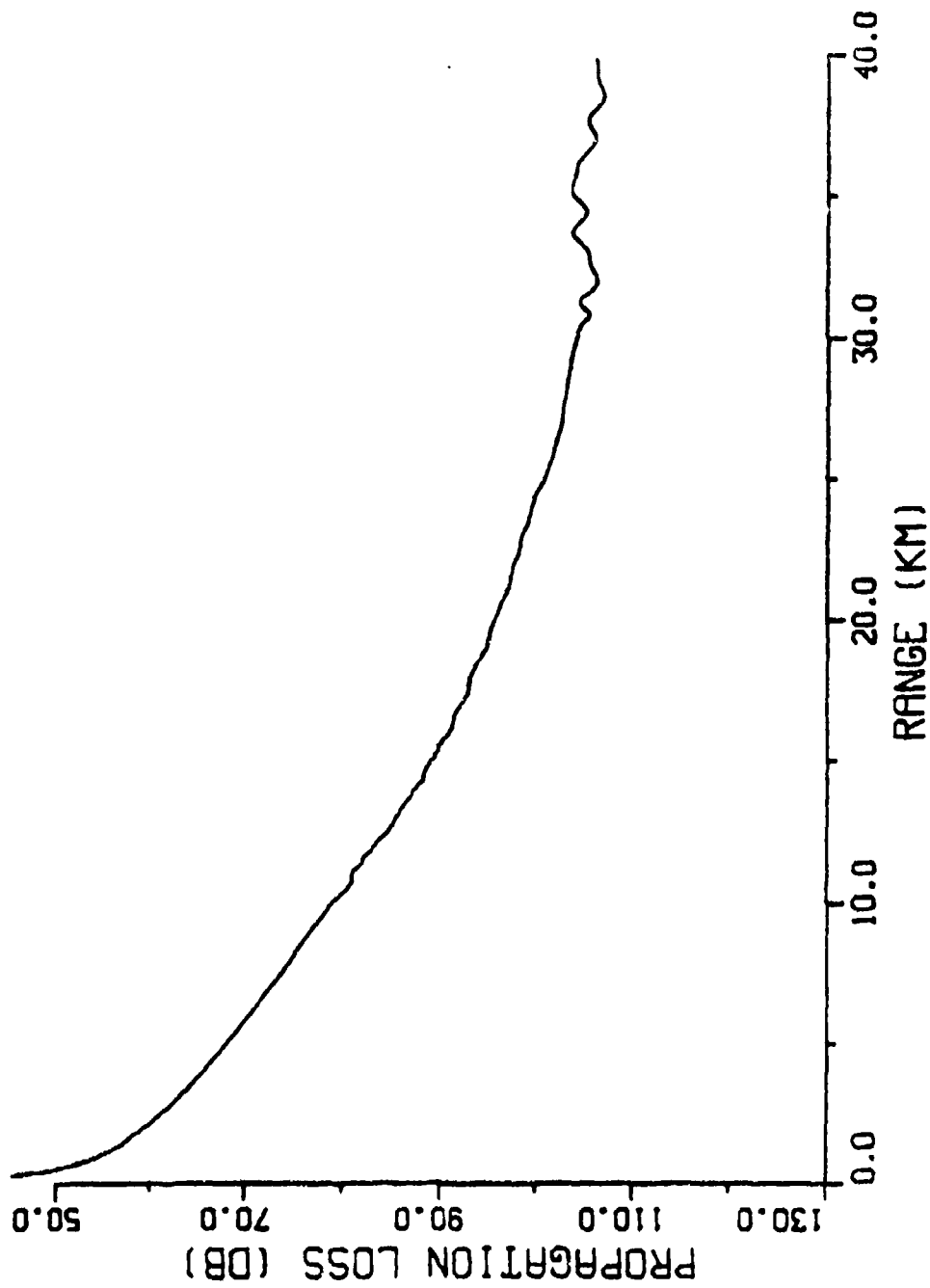


Figure 15. Propagation Loss Versus Range for Shallow-to-Deep Water Case, 0.85 degree Slope; IFD Results

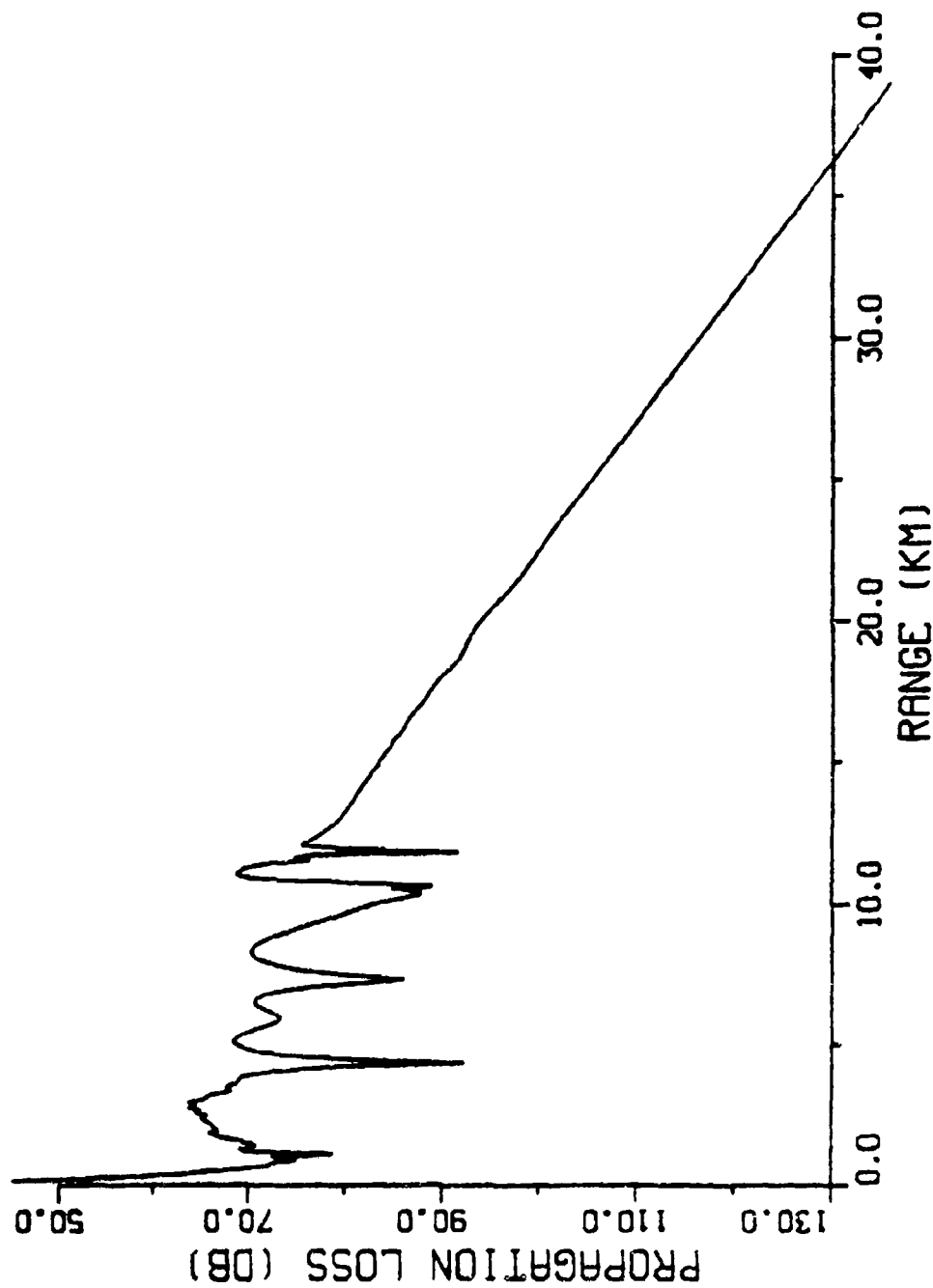


Figure 16. Propagation Loss Versus Range for Deep-to-Shallow Water Case, 8.5 degree Slope, 1.0 g/cm<sup>3</sup> Density in Sediment; IFD Results

turn results in more energy confined within the water layer. The difference in slope between the PAREQ and IFD results is attributed to the PAREQ program's apparent failure to account for the affects of the density discontinuity at the water-sediment interface. Because the IFD program correctly accounts for density discontinuities the results produced by IFD are believed to be more accurate than those of PAREQ when interface interaction is important.



## V. COMMENTS AND CONCLUSIONS

The IFD method is an efficient, stable method for solving the parabolic equation. Use of the IFD method is particularly advantageous in shallow water environments where the water-sediment interface is an important parameter.

The IFD program presented in this thesis incorporates continuity of pressure and continuity of the normal component of particle velocity across horizontal and sloping interfaces. The program's capability to incorporate the exact interface conditions on a sloping interface, to automatically determine step-size, and to modify the bottom as required for the case of a very gently sloping bottom are important features.

Projected program enhancements include wide angle propagation (Lee and Gilbert, 1982), range-dependent sound speed profiles in the water, range-dependent sound speed profiles in the sediment layer, and multiple sediment layers with horizontal or sloping interfaces. These enhancements are listed in their approximate order of importance. The program's modular construction and structured style will facilitate implementation of these enhancements.

# APPENDIX A: IMPLICIT FINITE-DIFFERENCE PROGRAM LISTING

```

*****
*** IMPLICIT FINITE-DIFFERENCE PROGRAM FOR
*** SOLVING THE PARABOLIC EQUATION
*****
*** LT LARRY JAEGER
*** U.S. NAVAL POSTGRADUATE SCHOOL
*** MONTEREY, CA 93943
*****
*** ALPHABETICAL LIST OF PROGRAM VARIABLES FOLLOWS:
*****
*** A - ARRAY - COEFFICIENT A IN PARABOLIC EQUATION
*** (IN WATER)
*** A2 - COEFFICIENT A IN PARABOLIC EQUATION (IN SEDIMENT)
*** ALPHA - VOLUME ATTENUATION - DB/METER
*** ATT - ARRAY - ATTENUATION COEFFICIENT FOR ARTIFICIAL
*** ATTENUATION LAYER
*** BEDA1 - BETA 1 AS DEFINED IN LEE AND MCCANIEL (1983)
*** BEDA2 - BETA 2 AS DEFINED IN LEE AND MCCANIEL (1983)
*** BETA1 - ATTENUATION IN WATER - DB/WAVELENGTH
*** BETA2 - ATTENUATION IN SEDIMENT - DB/WAVELENGTH
*** BR - ARRAY - RANGE FOR BOTTOM PROFILE - METERS
*** BZ - ARRAY - DEPTH FOR BOTTOM PROFILE - METERS
*** C - ARRAY - CONTAINS TRIANGULAR MATRIX SYSTEM THAT NEEDS
*** TO BE SOLVED (SEE SUBROUTINE TRIDG)
*** C0 - REFERENCE SPEED IN SEDIMENT
*** C2 - SOUND SPEED IN SEDIMENT
*** COSE - COS (THETA)
*** CR - ARRAY - STORAGE SPACE USED IN SUBROUTINES TRIDG AND
*** TRIDL
*** CSVP - SOUND SPEED IN SOUND SPEED PROFILE -
*** METERS/SEC
*** CTWO - ARRAY - STORAGE SPACE USED IN SUBROUTINES TRIDG AND
*** TRIDL
*** CHATER - SOUND SPEED AT GRID POINTS IN WATER COLUMN
*** DELTA - AS DEFINED IN LEE AND MCCANIEL (1983)
*** DELIN - DELTA
*** DR - RANGE STEP - METERS
*** DR1 - RANGE STEP ALONG LEVEL INTERFACE - METERS
*** DR2 - RANGE STEP ALONG LEVEL INTERFACE - METERS
*** DRMAX - MAXIMUM ALLOWABLE RANGE STEP - METERS
*** DZ - DEPTH INCREMENT OF SOLUTION - METERS
*** EYE - COMPLEXITY - I#
*** FRQ - FREQUENCY - HZ
*** GAMMA1 - GAMMA 1 AS DEFINED IN LEE AND MCCANIEL (1983)
*** GAMMA2 - GAMMA 2 AS DEFINED IN LEE AND MCCANIEL (1983)
*****

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*** IBO71 - POINTER THAT POINTS TO BOTTOM PROFILE POINT AT START
*** IBO72 - OF BOTTOM SEGMENT
*** IDFACE - OF BOTTOM SEGMENT
*** IFACE2 - ARRAY - RUN IDENTIFICATION
*** IFACEH - POINTER THAT POINTS TO INTERFACE AT RANGE RA1
*** IFACEP - IFACE
*** IPZ - IFACE + 1
*** ISLCPE - EVERY IPZTH VALUE IN DEPTH IS PRINTED
          SLOPE FLAG:
          ISLOPE = 1 - BOTTOM SLOPES DOWN
          ISLOPE = 2 - BOTTOM LEVEL
          ISLOPE = 3 - BOTTOM SLOPES UP
          ISLOPE = 4 - BOTTOM SLOPES DOWN, BOTTOM MODIFIED
          ISLOPE = 5 - BOTTOM SLOPES UP, BOTTOM MODIFIED
          TEMPORARY VARIABLE
          GRID POINT CORRESPONDING TO RECEIVER DEPTH
          NUMBER OF EQUI-SPACED GRID POINTS IN J
          INCLUDES BOTTOM POINT - DOES NOT INCLUDE SURFACE POINT
          NUMBER OF POINTS IN ARTIFICIAL ATTENUATION LAYER
          NUMBER OF POINTS IN BOTTOM PROFILE (BR AND BZ)
          UNIT NUMBER FOR INPUT DATA
          N - 1
          UNIT NUMBER FOR OUTPUT PLOTTER FILE
          UNIT NUMBER FOR OUTPUT PRINTER FILE
          UNIT NUMBER OF RANGE STEPS ALONG A BOTTOM SEGMENT
          NUMBER OF RANGE STEPS CORRESPONDING TO ONE VERTICAL
          GRID STEP FOR MODIFIED BOTTOM
          NUMBER OF POINTS IN CSVP AND ZSVP
          NUMBER OF GRID POINTS IN WATER AT MAX DEPTH
          NUMBER OF NEXT LEVEL SECTION FOLLOWING A SLOPING
          SECTION FOR A MODIFIED BOTTOM
          RANGE INCREMENT AT WHICH SOLUTION IS PASSED TO
          OUTPUT PRINTER FILE - METERS
          DEPTH INCREMENT AT WHICH SOLUTION IS PRINTED - METERS
          THE VALUE OF PI
          PROPAGATION LOSS - DB
          RANGE AT WHICH BOTTOM DEPTH IS AVAILABLE - METERS
          NEXT RANGE AT WHICH BOTTOM DEPTH IS AVAILABLE - METERS
          INCREMENT AS SOLUTION IS MARCHED OUT IN RANGE.
          RANGE AT WHICH SOLUTION IS KNOWN - METERS
          RANGE AT WHICH SOLUTION IS TO BE SOLVED - METERS
          ( RA2 = RA1 + OR )
          DENSITY IN WATER - GM/CM**3
          DENSITY IN SEDIMENT - GM/CM**3
          MAXIMUM RANGE OF SOLUTION - METERS
          SIN ( THETA )

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CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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*** TEMP - TEMPORARY VARIABLE - RADIANS
*** THETA - SLOPE OF BOTTOM - LEVEL INTERFACES DOWN
          - THETA > 0 - INTERFACES SLOPES UP
          - THETA < 0 - INTERFACES SLOPES DOWN
*** U - ARRAY - COMPLEX X ACOUSTIC PRESSURE FIELD
*** WDR - RANGE - STEP AT WHICH SOLUTION IS WRITTEN TO OUTPUT
          - PLOTTER FILE
*** XK0 - REFERENCE WAVE NUMBER
*** XLI - MATRIX ELEMENT, X MATRIX, LOWER DIAGONAL, ON INTERFACE
*** XLIZ - MATRIX ELEMENT, X MATRIX, LOWER DIAGONAL, ON INTERFACE
*** XLAHQA - XLI FOR SLOPING BOTTOM
*** XLRW5 - REFERENCE WAVELENGTH - METERS
          - MATRIX ELEMENT, X MATRIX, OFF-DIAGONAL, IN WATER AND
          - SEDIMENT
*** XMI - ELEMENT, X MATRIX, MAIN DIAGONAL, ON INTERFACE
*** XMS - ELEMENT, X MATRIX, MAIN DIAGONAL, ON INTERFACE
*** XMH - MATRIX ELEMENT, X MATRIX, MAIN DIAGONAL, IN SEDIMENT
          - MATRIX ELEMENT, X MATRIX, MAIN DIAGONAL, IN
          - WATER
*** XN - REAL INDEX OF REFRACTION
*** XNI - COMPLEX INDEX OF REFRACTION SQUARED
*** XPR - RANGE AT WHICH SOLUTION IS PRINTED - METERS
*** XWR - RANGE AT WHICH SOLUTION IS WRITTEN TO OUTPUT
          - PLOTTER FILE
*** XX... - VARIABLES THAT BEGIN WITH XX HAVE NO SPECIAL PHYSICAL
          - SIGNIFICANCE BUT THEY CONTRIBUTE TO COMPUTATIONAL
          - EFFICIENCY. ALL XX VARIABLES ARE CALCULATED IN
          - SUBROUTINE INITIAL, ALL ARE INDEPENDENT OF RANGE STEP
          - AND INTERFACE SLOPE, AND ALL ARE USED TO CALCULATE
          - MATRIX ELEMENTS.
*** YLI - MATRIX ELEMENT, Y MATRIX, LOWER DIAGONAL, ON INTERFACE
*** YLIV - MATRIX ELEMENT, Y MATRIX, LOWER DIAGONAL, ON INTERFACE
*** YLIZ - YLI FOR LEVEL INTERFACES
*** YLRW5 - MATRIX FOR SLOPING INTERFACES
          - SEDIMENT
*** YMI - MATRIX ELEMENT, Y MATRIX, MAIN DIAGONAL, ON INTERFACE
*** YMS - MATRIX ELEMENT, Y MATRIX, MAIN DIAGONAL, ON INTERFACE
*** YMH - MATRIX ELEMENT, Y MATRIX, MAIN DIAGONAL, IN SEDIMENT
          - MATRIX ELEMENTS, Y MATRIX, MAIN DIAGONAL, IN
          - WATER
*** YRI - MATRIX ELEMENT, Y MATRIX, UPPER DIAGONAL, ON INTERFACE
*** YRIV - MATRIX ELEMENT, Y MATRIX, UPPER DIAGONAL, ON INTERFACE
*** YRIZ - YRI FOR LEVEL INTERFACES
*** Z1 - DEPTH OF WATER AT RANGE R1 - METERS
*** Z2 - DEPTH OF WATER AT RANGE R2 - METERS
*** ZABLYR - DEPTH OF UPPER EDGE OF ARTIFICIAL ATTENUATION
          - LAYER - METERS
*** ZI - DEPTH OF GRID POINT - METERS
*** ZLYR1 - MAXIMUM WATER DEPTH - METERS
*** ZLYR2 - DEPTH OF PRESSURE RELEASE SURFACE - METERS

```

```

CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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*** ZR      - RECEIVER DEPTH - METERS
*** ZS      - SOURCE DEPTH - METERS
*** ZSVP    - ARRAY - DEPTH FOR SOUND SPEED PROFILE - METERS
*** ZZ...   - VARIABLES THAT BEGIN WITH ZZ HAVE NO SPECIAL PHYSICAL
              SIGNIFICANCE BUT THEY CONTRIBUTE TO COMPUTATIONAL
              EFFICIENCY. ALL ZZ VARIABLES ARE CALCULATED IN
              SUBROUTINE NEWMAT. ALL DEPEND ON RANGE STEP AND/OR
              INTERFACE SLOPE, AND ALL ARE USED TO CALCULATE MATRIX
              ELEMENTS.
*****
*** INPUT
*****
INPUT UNIT NUMBER = NIU
INPUT FILENAME AND FILETYPE = IFOIN.DATIN
CONTENTS:
CARD 1 : FRQ, ZS, ZR, CO, N
CARD 2 : RMAX, DRLVL, DRMAX, WDR, PDR, PDZ
CARD 3 : BR(1), BZ(1)
CARD 4 : BR(2), BZ(2)
*****
CARD N : -1, -1, RHO1, BETA1
CARD N+1 : ZLYR(1), CSVP(1)
CARD N+2 : ZSVP(1), CSVP(1)
CARD N+3 : ZSVP(2), CSVP(2)
CARD N+4 : ZSVP(2), CSVP(2)
*****
CARD N+M : ZSVP(J), CSVP(J)
CARD N+M+1 : ZLYR2, RHO2, BETA2, C2
CARD N+M+2 : ZABLYR
*****
WHERE:
FRQ = FREQUENCY (HZ)
ZS = SOURCE DEPTH (M)
ZR = RECEIVER DEPTH (M)
CO = REFERENCE SOUND SPEED (M/S). IF CO = 0.0, CO IS
    SET TO AVERAGE SOUND SPEED IN WATER COLUMN.
N = NUMBER OF GRID POINTS
*****
RMAX = MAXIMUM RANGE (M) OF SOLUTION INTERFACE. IF
DRLVL = RANGE STEP (M) ALONG LEVEL INTERFACES. IF
      DRLVL = 0.0, DRLVL SET TO 1/2 WAVELENGTH. IF
      DRLVL GREATER THAN DRMAX, DRLVL SET TO DRMAX.
DRMAX = MAXIMUM ALLOWABLE RANGE STEP (M). IF DRMAX = 0.0,
      DRMAX IS SET TO ONE WAVELENGTH.
WDR = RANGE STEP (M) AT WHICH SOLUTION IS WRITTEN TO
      FILE USED BY PLOTTING ROUTINE.

```

CC



[illegible]

```

IFD002890
IFD002900
IFD002910
IFD002920
IFD002930
IFD002940
IFD002950
IFD002960
IFD002970
IFD002980
IFD002990
IFD003000
IFD003010
IFD003020
IFD003030

```

```

C      IF (RA2P.GE.XMR) CALL WRITE2
C      *** TIME TO PRINT?
C      IF (RA2P.GE.XPR) CALL PRINT2
C      *** TIME TO TERMINATE?
C      IF (RA2.GE.RMAX) GO TO 90
C      80
C      CONTINUE
C      *** GO BACK AND CONTINUE WITH NEXT LINEAR BOTTOM SEGMENT
C      GO TC 1C
C      *** TIME TO TERMINATE
C      CALL ENC (RA2)
C      90
C      STOP
C      END

```



```

SUBROUTINE READ
(1) THIS SUBROUTINE READS ALL INPUT DATA
(2) THE DATA IS READ FROM INPUT UNIT NUMBER: NIU = 51
(3) INPUT FILENAME AND FILETYPE ARE: IFDIN DATAIN
(4) DATA IS READ IN FREE FORMAT.
(5) DATA IS TRANSFERRED BACK TO MAIN PROGRAM VIA COMMON BLOCK

COMMON /IN/ IA,IBOT1,IFACE,IPZ,ISLOPE,ISTEP,IMZ,N,NA,NBOT,NM1,
* NSTEP,NSTEP1,NSVP,NMAX,NXLFS
COMMON /REAL/ ALPHA,ATT(5000),BETA1,BETA2,BR(101),BZ(101),CO,
* CSVP(101),C,CHATER(5000),DR,DRVL,DRMAX,DZ,FRQ,PDR,PDZ,
* RI,RAI,RA2,RHO1,RHO2,RMAX,THEIA,XKO,XLAMD,XPR,XX4,XX15,
* XX11,XMR,WDR,ZLYR1,ZLYR2,ZR,ZS,ZSVP(101),ZABLYR
DATA NIU/51/, NPOUT/55/

*** READ INPUT PARAMETERS
READ(NIU,*,END=100) FRQ, ZS, ZR, CO, N
READ(NIU,*,END=100) RMAX, DRVL, DRMAX, WDR, PDR, PDZ

*** READ BOTTOM PROFILE - RANGE, DEPTH
DO 10 I=1,101
  READ(NIU,*,END=100) BR(I), BZ(I)
  NBOT=I
  *** END OF PROFILE?
  *** IF(BR(1).LT.0.0) GO TO 20
  *** NO
  CONTINUE

CONTINUE
*** EXTEND LAST DEPTH BEYOND MAX RANGE
BR(NBOT) = 1.0E+10
BZ(NBOT) = BZ(NBOT-1)

*** FIRST LAYER IS WATER, SECOND IS SEDIMENT.
*** READ MAX DEPTH, DENSITY AND ATTENUATION OF FIRST LAYER
READ(NIU,*,END=100) ZLYR1, RHO1, BETA1

*** READ SOUND SPEED PROFILE IN FIRST LAYER
DO 25 I=1,101
  NSVP=I
  READ(NIU,*,END=100) ZSVP(I), CSVP(I)
  *** READ ANOTHER PROFILE POINT?
  *** IF(ZSVP(I).LT.ZLYR1) GO TO 25
  *** NO
  *** HAS THAT THE LAST PROFILE PCINT?
  *** IF(ZSVP(I).EQ.ZLYR1) GO TO 30
  *** NO, THERE IS ERROR.

```

```

25      GO TO 101
C      CONTINUE
C      *** DOES THE SOUND SPEED PROFILE START AT THE SURFACE?
C      IF ( ZSVP(1).NE.0.0 ) GO TO 102
C      *** YES
C      *** READ DEPTH, DENSITY, ATTENUATION AND SPEED IN SECOND LAYER
C      READ(NIL,*,END=100) ZLYR2, RHO2, BETA2,C2
C      *** READ DEPTH OF UPPER EDGE OF ARTIFICIAL ATTENUATING LAYER
C      REAC(NIU,*,END=100) ZABLYR
C      RETURN
C      *** ERROR EXISTS
C      WRITE(6,500)
C      WRITE(NPOUT,900)
C      STOP
101     WRITE(6,901)
C      WRITE(NPOUT,901)
C      STOP
102     WRITE(6,502)
C      WRITE(NPOUT,902)
C      STOP
C      900     FORMAT(//,1X,'ERROR: EXPECTING MORE INPUT DATA.',/,9X,
C      901     * 'EXECUTION TERMINATED.',//)
C      901     * FORMAT(//,1X,'ERROR: FINAL DEPTH IN SOUND SPEED PROFILE DOES NOT
C      901     * //,9X,'EQUAL MAXIMUM DEPTH OF WATER COLUMN.',/,9X,
C      902     * 'EXECUTION TERMINATED.',//)
C      902     * FORMAT(//,1X,'ERROR: FIRST DEPTH IN SOUND SPEED PROFILE
C      902     * //,9X,'DOES NOT EQUAL ZERO.',/,9X,
C      902     * 'EXECUTION TERMINATED.',//)
C      END

```

```

READ00490
READ00500
READ00510
READ00520
READ00530
READ00540
READ00550
READ00560
READ00570
READ00580
READ00590
READ00600
READ00610
READ00620
READ00630
READ00640
READ00650
READ00660
READ00670
READ00680
READ00690
READ00700
READ00710
READ00720
READ00730
READ00740
READ00750
READ00760
READ00770
READ00780
READ00790
READ00800
READ00810
READ00820

```

```

SUBROUTINE SVPM
  (1) THIS SUBROUTINE CALCULATES THE VERTICAL STEP SIZE: DZ
  (2) THIS SUBROUTINE ALSO CALCULATES THE SPEED OF SOUND AT
  EACH OF THE VERTICAL GRID POINTS.
  (3) SOUND SPEEDS ARE DETERMINED BY LINEAR INTERPOLATION.
  (4) SOUND SPEEDS ARE STORED IN CWATER(I).
  (A) THE INDEX I RANGES FROM 1 TO NMAX.
  (B) CWATER(I) CORRESPONDS TO THE GRID POINT DZ BELOW
      THE SURFACE.

  COMMON /IN/ IA, I60T1, IFACE, IPZ, ISLOPE, ISTEP, IMZ, N, NA, NBOT, NML,
  * NSTEP, NSTEP1, NSVP, NMAX, NX1, LFS
  * COMMON /REAL/ ALPHA, ATT(500), BETA1, BETA2, BR(101), BZ(101), CO,
  * CSVP(101), C2, CWATER(500), D, DR, DRVL, CRMAX, DZ, FRQ, PDR, PDZ,
  * R1, RAL, RA2, RH01, RH02, RMAX, THETA, XKO, XLAMDA, XPR, XX4, XX10,
  * XX11, XWR, WDR, ZLYR1, ZLYR2, ZR, ZS, ZSVP(101), ZABLYR

  **CALCULATE VERTICAL STEP SIZE
  DZ = ZLYR2 / FLOAT(N)

  **CALCULATE NUMBER OF GRID POINTS IN WATER COLUMN
  NMAX = INT((ZLYR1/DZ)+0.5)

  **CALCULATE SOUND SPEED AT ALL GRID POINTS IN WATER COLUMN
  L=1
  DO 20 I=1, NMAX
    ZI = I*DZ
    LP1 = L+1
    **NEED TO UPDATE PROFILE ENDPOINTS?
    IF (ZI.LE.ZSVP(LP1)) GO TO 10
    **YES
    L = L+1
    LP1 = L+1
    CWATER(I) = (CSVP(LP1) - CSVP(L)) * (ZI - ZSVP(L)) /
    * (ZSVP(LP1) - ZSVP(L))
  10
  20
  CONTINUE
  RETURN
  END

```

```

SUBROUTINE INITIAL
  (1) THIS SUBROUTINE INITIALIZES CONSTANTS AND VARIABLES.
  (2) VALUES ARE TRANSFERRED TO FROM MAIN PROGRAM VIA COMMON
      BLOCK.

COMMON /IN/ IA, IBOT1, IFACE, IPZ, ISLCPE, ISTEP, INZ, N, NA, NBGT, NML,
* NSTEP, NSTEP1, NSVP, NMAX, NXLFS
COMMON /REAL/ ALPHA, ATT(5000), BETA1, BETA2, BR(101), BZ(101), CO,
* CSVP(101), C2, CWAIR(5000), DRLVL, DRMAX, DZ, FRQ, PDR, PDZ,
* R1, RAL, RA2, RH01, RH02, RMAX, THETA, XK0, XLAMDA, XPR, XX4, XX10,
* XXI1, XWR, XDR, ZLYR1, ZLYR2, ZR, ZS, ZSVP(101), ZABLYR
* DATA PI/3.141592654/

*** IF CO NOT SPECIFIED, SET CO TO AVERAGE SPEED IN WATER COLUMN
*** (USING MAX DEPTH PROFILE)
IF(CO.NE.0.0) GO TO 11
DO 10 I=2, NSVP
  CO=CO+ZSVP(I)-ZSVP(I-1)*(CSVP(I-1) +
* 0.5*(CSVP(I)-CSVP(I-1)))
  CONTINUE
CO = CO/ZSVP(NSVP)
CONTINUE

*** INITIALIZE RANGE
RAL = 0.0

*** INITIALIZE POINTER THAT POINTS TO BOTTOM PROFILE POINT
IBOT1 = 0

*** COMPUTE REFERENCE WAVE NUMBER
XK0 = 2.0*PI*FRQ/CO

*** COMPUTE REFERENCE WAVELENGTH
XLAMDA = CO/FRQ

*** IF DRLVL=0 SET DRLVL EQUAL TO 1/2 REFERENCE WAVELENGTH
IF ( DRLVL.EQ.0.0 ) DRLVL = 0.5 * XLAMDA

*** IF DRMAX=0 SET DRMAX EQUAL TO REFERENCE WAVELENGTH
IF ( DRMAX.EQ.0.0 ) DRMAX = XLAMDA

*** IF DRLVL GREATER THAN DRMAX SET DRLVL EQUAL TO DRMAX
IF (DRLVL.GT.DRMAX) DRLVL = DRMAX

*** COMPUTE ATTENUATION - SACLANT MEMO SM-121 (JENSEN + FERLA)
*** MODIFIED AS FOLLOWS:
*** IF INPUTTED BETA IS LT 0.0, ALPHA IS COMPUTED IN DB/METER

```

INI00490  
 INI00500  
 INI00510  
 INI00520  
 INI00530  
 INI00540  
 INI00550  
 INI00560  
 INI00570

```

C      *** AND USEC FOR BETA
      *  ALPHA=FRQ*FRQ*(.007+(.155*1.71/(1.7*1.7+FRQ*FRQ*.000011))
      *  *1.0E-09
C      *** INITIALIZE POINTER THAT POINTS TO INTERFACE GRID POINT
      *  IFACE = INT ( BZ(1)/DZ + 0.5 )
C      RETURN
      END

```



MAT00C490  
 MAT000500  
 MAT000510  
 MAT000520  
 MAT000530  
 MAT000540  
 MAT000550  
 MAT000560  
 MAT000570  
 MAT000580  
 MAT000590  
 MAT000600  
 MAT000610  
 MAT000620  
 MAT000630  
 MAT000640  
 MAT000650

```

*** THIS SECTION PERTAINS TO POINTS IN WATER COLUMN
DO 10 I=1,NMAX
*** CALCULATE REAL INDEX OF REFRACTION IN WATER
*** XN = CO/CWATER(I)
*** CALCULATE ATTENUATION AS PER COMMENTS IN SUBROUTINE
*** IF (BETAL-LI*0.01) BETAL = ALPHA*CWATER(I)/FRQ
*** CALCULATE COMPLEX INDEX OF REFRACTION SQUARED
*** (SEE PAGE 2-11 IN TR 6659)
*** XN1 = CMPLX ( XN*XN , XN*XN*BETAL/27.287527 )
*** CALCULATE COEFFICIENT A(I)
*** A(I) = 0.5 * EYE * XK0 * (XN1-1.0)
*** CALCULATE XX1M
*** XX1M(I) = 0.5 * A(I) - XX2
      CCNTINE
    RETURN
  END
  
```

10

```

SUBROUTINE SFIELD(FRQ,CO,ZS,N,DZ,U)
*** THIS SUBROUTINE IS IDENTICAL TO SUBROUTINE SFIELD AS PER
*** NUSC TECHNICAL REPORT 6659.
*****
*** GAUSSIAN STARTING FIELD - SEE NORDA TECH NOTE 12 BY H.K.BROCK
*****
*** CALLING ROUTINE SUPPLIES:
FRQ - FREQUENCY IN HZ
CO - REFERENCE SOUND SPEED - METERS/SEC
ZS - DEPTH OF SOURCE IN METERS.
N - NUMBER OF POINTS IN ARRAY U
DZ - DEPTH INCREMENT - METERS
*** SFIELD SUBROUTINE SUPPLIES:
U - COMPLEX STARTING FIELD
*****
COMPLEX U(1)
DATA PI/3.1415926535/
THE FIELD IS DEFINED AS A GAUSSIAN BEAM AT RANGE = 0.
LOCAL VARIABLES - GA GAUSSIAN AMPLITUDE
XK0=2.0*PI*FRQ/CO
GW=2.0/XK0
GA=SQR(GW)/GW
DO 10 I=1,N
ZM=I*DZ
PR=GAUSS(GA,ZM,ZS,GW)-GAUSS(GA,-ZM,ZS,GW)
U(I)=CMFLX(PR,0.0)
CONTINUE
RETURN
END
FUNCTION GALSS(GA,Z,GD,GW)
INPUT - GA GAUSSIAN AMPLITUDE
OUTPUT - GALSS = GA * EXP(-(Z - GD) / GW)**2)
TEMPORARY VARIABLE - V
V=(Z-GD)/GW
V=-(V*V)
GAUSS=GA*EXP(V)
RETURN
END

```

SF100010  
SF100020  
SF100030  
SF100040  
SF100050  
SF100060  
SF100070  
SF100080  
SF100090  
SF100100  
SF100110  
SF100120  
SF100130  
SF100140  
SF100150  
SF100160  
SF100170  
SF100180  
SF100190  
SF100200  
SF100210  
SF100220  
SF100230  
SF100240  
SF100250  
SF100260  
SF100270  
SF100280  
SF100290  
SF100300  
SF100310  
SF100320  
SF100330  
SF100340  
SF100350  
SF100360  
SF100370  
SF100380  
SF100390  
SF100400  
SF100410  
SF100420  
SF100430

CCCCCCCCCCCCCCCC

CCC

10

CCC



```

SUBROUTINE WRITE1
(1) THIS SUBROUTINE OUTPUTS UNFORMATTED DATA TO A FILE
    THAT IS USED BY THE PLOTTING ROUTINE.
(2) THE FILE CORRESPONDS TO UNIT FILE NUMBER: NOU = 52
(3) THE FILENAME AND FILETYPE FOR THIS FILE ARE:
    IFDCUT PLOTTER

COMPLEX A(2,C), CR, CTWO, EYE,
        XLI, XLI2, XLRWS, XMI, XMS, XRI, XRI2,
        XX1, XX2, XX3, XX4, XX5, XX6, XX7, XX8, XX9, XX12, XX1M,
        VLI, VLI2, VLI3, VLI4, VLI5, VLI6, VLI7, VLI8, VLI9, VLI10, VLI11, VLI12, VLI13, VLI14, VLI15, VLI16, VLI17, VLI18, VLI19, VLI20, VLI21, VLI22, VLI23, VLI24, VLI25, VLI26, VLI27, VLI28, VLI29, VLI30,
        U, Z25, Z26, Z27, Z28, Z29, Z30, Z31, Z32, Z33, Z34, Z35, Z36, Z37, Z38, Z39, Z40, Z41, Z42, Z43, Z44, Z45, Z46, Z47, Z48, Z49, Z50, Z51, Z52, Z53, Z54, Z55, Z56, Z57, Z58, Z59, Z60, Z61, Z62, Z63, Z64, Z65, Z66, Z67, Z68, Z69, Z70, Z71, Z72, Z73, Z74, Z75, Z76, Z77, Z78, Z79, Z80, Z81, Z82, Z83, Z84, Z85, Z86, Z87, Z88, Z89, Z90, Z91, Z92, Z93, Z94, Z95, Z96, Z97, Z98, Z99, Z100,
        /IN/ IA, IBOT, IFACE, IP2, ISLOPE, ISTEP, IWZ, N, NA, NBOT, NM1,
        /NSTEP/ NSTEP1, NSTEP2, NSTEP3, NSTEP4, NSTEP5, NSTEP6, NSTEP7, NSTEP8, NSTEP9, NSTEP10, NSTEP11, NSTEP12, NSTEP13, NSTEP14, NSTEP15, NSTEP16, NSTEP17, NSTEP18, NSTEP19, NSTEP20, NSTEP21, NSTEP22, NSTEP23, NSTEP24, NSTEP25, NSTEP26, NSTEP27, NSTEP28, NSTEP29, NSTEP30, NSTEP31, NSTEP32, NSTEP33, NSTEP34, NSTEP35, NSTEP36, NSTEP37, NSTEP38, NSTEP39, NSTEP40, NSTEP41, NSTEP42, NSTEP43, NSTEP44, NSTEP45, NSTEP46, NSTEP47, NSTEP48, NSTEP49, NSTEP50, NSTEP51, NSTEP52, NSTEP53, NSTEP54, NSTEP55, NSTEP56, NSTEP57, NSTEP58, NSTEP59, NSTEP60, NSTEP61, NSTEP62, NSTEP63, NSTEP64, NSTEP65, NSTEP66, NSTEP67, NSTEP68, NSTEP69, NSTEP70, NSTEP71, NSTEP72, NSTEP73, NSTEP74, NSTEP75, NSTEP76, NSTEP77, NSTEP78, NSTEP79, NSTEP80, NSTEP81, NSTEP82, NSTEP83, NSTEP84, NSTEP85, NSTEP86, NSTEP87, NSTEP88, NSTEP89, NSTEP90, NSTEP91, NSTEP92, NSTEP93, NSTEP94, NSTEP95, NSTEP96, NSTEP97, NSTEP98, NSTEP99, NSTEP100,
        /REAL/ ALPHA, ATT(5000), BETA1, BETA2, BR(101), BZ(101), CO,
        /CSVP(101), C2, CWATER(5000), DR, DRLVL, CRMAX, DZ, FRQ, PDK, PDZ,
        RI, RAI, RA2, RH01, RH02, RMAX, THETA, XKO, XLAMDA, XPR, XX4, XX10,
        XXI1, XWR, WDR, ZLYR1, ZLYR2, ZR, ZS, ZSVP(101), ZABLYR,
        /CPLX/ A(5000), A2, C(5000), C1, CRI, XRI2,
        EYE, XLI, XLI2, XLRWS, XMI, XMS, XRI, XRI2, XX1M(5000),
        XX1, XX2, XX3, XX4, XX5, XX6, XX7, XX8, XX9, XX12, XLI2, XLI3, XLI4, XLI5, XLI6, XLI7, XLI8, XLI9, XLI10, XLI11, XLI12, XLI13, XLI14, XLI15, XLI16, XLI17, XLI18, XLI19, XLI20, XLI21, XLI22, XLI23, XLI24, XLI25, XLI26, XLI27, XLI28, XLI29, XLI30,
        XLI, VLI, VLI2, VLI3, VLI4, VLI5, VLI6, VLI7, VLI8, VLI9, VLI10, VLI11, VLI12, VLI13, VLI14, VLI15, VLI16, VLI17, VLI18, VLI19, VLI20, VLI21, VLI22, VLI23, VLI24, VLI25, VLI26, VLI27, VLI28, VLI29, VLI30,
        U(5000), Z25, Z26, Z27, Z28, Z29, Z30, Z31, Z32, Z33, Z34, Z35, Z36, Z37, Z38, Z39, Z40, Z41, Z42, Z43, Z44, Z45, Z46, Z47, Z48, Z49, Z50, Z51, Z52, Z53, Z54, Z55, Z56, Z57, Z58, Z59, Z60, Z61, Z62, Z63, Z64, Z65, Z66, Z67, Z68, Z69, Z70, Z71, Z72, Z73, Z74, Z75, Z76, Z77, Z78, Z79, Z80, Z81, Z82, Z83, Z84, Z85, Z86, Z87, Z88, Z89, Z90, Z91, Z92, Z93, Z94, Z95, Z96, Z97, Z98, Z99, Z100,
        DATA NOU/52,

** WRITE MAXIMUM RANGE
WRITE(NCU,*) RMAX

** INITIALIZE RANGE VARIABLE AT WHICH SOLUTION IS TO BE RECORDED
XWR = RAI+WDR

** COMPUTE RECEIVER DEPTH TO NEAREST DZ
IF (ZR.LT.DZ) ZR = DZ
IWZ = ZR/DZ + 0.5
ZR = IWZ*DZ

** WRITE STARTING VALUE
WRITE(NCU,*) RAI, ZR, U(IWZ)

RETURN
END

```

```

WR100010
WR100020
WR100030
WR100040
WR100050
WR100060
WR100070
WR100080
WR100090
WR100100
WR100110
WR100120
WR100130
WR100140
WR100150
WR100160
WR100170
WR100180
WR100190
WR100200
WR100210
WR100220
WR100230
WR100240
WR100250
WR100260
WR100270
WR100280
WR100290
WR100300
WR100310
WR100320
WR100330
WR100340
WR100350
WR100360
WR100370
WR100380
WR100390
WR100400
WR100410
WR100420

```

CCCCCCCC

CC C C C C C C

```

SUBROUTINE PRINT1
(1) THIS SUBROUTINE OUTPUTS FORMATTED DATA TO A FILE
    WHICH IS READY TO BE SENT TO THE PRINTER.
(2) THE FILE C CORRESPONDS TO UNIT FILE NUMBER: NPOUT = 55
(3) THE FILENAME AND FILETYPE FOR THIS FILE ARE:
    IFDOUT
    PRINTER

DIMENSION IC(17)
COMMON /IN/ IA,IBOT1,IFACE,IPZ,ISLOPE,ISTEP,JWZ,N,NA,NBOT,NM1,
* NSTEP,NSTEP1,NSVP,NWMAX,NXLFS
COMMON /REAL/ ALPHA,ATT(5000),BETA1,BETA2,BR(101),BZ(101),CO,
* CSVP(101),C2,CWATER(5000),DR,DRVLV,DRMAX,ZZ,FRQ,PDR,PDZ,
* RI,RA1,RA2,RHO1,RHO2,RMAX,THETA,XKO,XLAMD,XPR,XX4,XX10,
* XXI,XXWR,WDR,ZLYR1,ZLYR2,ZR,ZS,ZSVP(101),ZABLYR
DATA NPCLT/55/

*** PROMPT USER FOR RUN IDENTIFICATION
WRITE(6,890)
*** READ USER RESPONSE
READ(5,891) ( ID(I), I=1,16 )

*** PRINT SELECTED PARAMETERS OF INTEREST
WRITE(NPOUT,900) (ID(I), I=1,16), FRQ, ZS, ZR, DZ, CO, XKO, N
*

*** PRINT SOUND SPEED PROFILE IN WATER
WRITE(NPOUT,904)
DO 5 I=1,NSVP
  WRITE(NPOUT,905) ZSVP(I), CSVP(I)
CONTINUE

*** PRINT MORE SELECTED PARAMETERS OF INTEREST
WRITE(NPOUT,901) ZLYR1, RHO1, BETA1, ZLYR2, RHO2, BETA2, C2

*** PRINT BOTTOM PROFILE
WRITE(NPOUT,902)
NBOTM1 = NBCT-1
DO 10 I=1,NBOTM1
  WRITE(NPOUT,903) BR(I), BZ(I)
CONTINUE

*** COMPUTE DEPTH PRINT INCREMENT TO NEAREST DZ
IPZ = INT ( PDZ/DZ+0.5 )
IF ( IPZ.EQ.0 ) IPZ = 1

*** INITIALIZE RANGE VARIABLE AT WHICH SOLUTION IS TO BE PRINTED
XPR = RA1+PCR

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 NEW000480

# SUBROUTINE NEWSEG

THIS SUBROUTINE IS CALLED AT THE START OF EACH NEW BOTTOM  
 SEGMENT. THE SUBROUTINE DOES THE FOLLOWING TASKS FOR EACH  
 BOTTOM SEGMENT:

- (1) UPDATES BOTTOM PROFILE POINTERS: IBO11 & IBO12
- (2) COMPUTES SLOPE: THETA
- (3) COMPUTES NUMBER OF RANGE STEPS IN SEGMENT: NSTEP
- (4) COMPUTES RANGE STEP: DR
- (5) SETS SLOPE FLAG: ISLOPE
- (6) INITIALIZES RANGES: RAL & RA2
- (7) CHECKS THAT RANGE STEP IS LESS THAN OR MAX
- (8) ISSUES ERROR OR WARNING MESSAGES AS APPROPRIATE

```

COMMON /IN/ IA, IBO11, IFACE, IPZ, ISLOPE, ISTEP, INZ, N, NA, NBO1, NML,
* NSTEP, NSTEP1, NSVP, NMAX, NMAX1, NMAX2, BZ(101), BZ(101), CO,
* /REAL/ ALPHA, AT(500), BETAI, BETI2, BZ(101), BZ(101), CO,
* /CSV/ (101), C2, C2ATER(500), DR, DRVL, DRMAX, DZ, FRQ, PDR, PDZ,
* RI, RAI, RA2, RH01, RH02, RMAX, THETA, XK0, XLAMDA, XPR, XX4, XX10,
* XX11, XWR, WDR, ZLV1, ZLV2, ZR, ZS, ZSVP(101), ZABLYR
DATA NPCUT/55/
  
```

## \*\*\* UPDATE BOTTOM PROFILE POINTER

```

IBO11 = IBO11 + 1
IBO12 = IBO11 + 1
GET STARTING AND ENDING RANGES AND DEPTHS FOR THIS SEGMENT
  
```

```

R1 = BR(IBO11)
R2 = BZ(IBO11)
Z1 = BZ(IBO12)
Z2 = BZ(IBO12)
** ERR CR CHECK
** IF (R2 - LE, R1) GO TO 100
** PUT Z1 AND Z2 ON NEAREST GRID PCINTS
** ITEMP = INT ( Z1/DZ + 0.5 )
** Z1 = DZ * FLOOR ( ITEMP )
** ITEMP = INT ( Z2/DZ + 0.5 )
** Z2 = DZ * FLOOR ( ITEMP )
  
```

```

*** COMPUTE SLOPE
*** THETA = ATAN2 (Z2 - Z1, R2 - R1)
*** DOES BOTTOM SLOPE DOWN, LEVEL OR UP?
*** IF (THETA.GT.0.0) GO TO 10
*** IF (THETA.LT.0.0) GO TO 20
  
```

```

C *** BOTTOM IS LEVEL
C *** DETERMINE NUMBER OF RANGE STEPS FOR SEGMENT
C *** NSTEP = INT ( (R2-R1)/DRVL + 0.9999 )
C *** DETERMINE RANGE STEP
C *** DR = (R2-R1) / FLOAT(NSTEP)
C *** SET ISLOPE
C *** ISLOPE = 2
C GC TC 80

C *** BOTTOM SLOPES DOWN
C *** DETERMINE NUMBER OF RANGE STEPS
C *** NSTEP = INT ( (Z2-Z1+0.05)/DZ )
C *** DETERMINE RANGE STEP
C *** DR = (R2-R1)/FLOAT(NSTEP)
C *** SET ISLOPE
C *** ISLOPE = 1
C GC TC 30

C *** BOTTOM SLOPES UP
C *** DETERMINE NUMBER OF RANGE STEPS
C *** NSTEP = INT ( (Z1-Z2+0.05)/DZ )
C *** DETERMINE RANGE STEP
C *** DR = (R2-R1)/FLOAT(NSTEP)
C *** SET ISLOPE
C *** ISLOPE = 3
C GC TC 30

C *** IS RANGE STEP TOO LARGE?
C *** IF ( DR.LE.DRMAX ) GO TO 80
C *** YES, BOTTOM MUST BE MODIFIED
C *** SET ISLOPE
C *** ISLOPE = 4
C *** IF ( THETA.LT.0.0 ) ISLOPE = 5
C *** DETERMINE GRID POINT
C *** NSTEPI = INT ( DR/DRMAX + 0.9999 )
C *** DETERMINE RANGE STEP
C *** DR = DR / FLOAT(NSTEPI)
C *** REDETERMINE NUMBER OF RANGE STEPS
C *** NSTEP = NSTEP * NSTEPI
C *** COMPUTE SLOPE OF SLOPING SECTION
C *** THETA = ATAN2(DZ,DR)
C *** SLOPING SECTION
C *** NXLFS = NSTEPI/2 + 2
C *** INDICATE TO USER THAT BOTTOM HAS BEEN MODIFIED
C *** TEMP = 0.5 * DZ
C *** WRITE(6,903) R1,R2,TEMP

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C      C570
NEW00980
NEW00990
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NEW01010
NEW01020
NEW01030
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NEW01210
NEW01220
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NEW01240
NEW01250
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NEW01270
NEW01280
NEW01290
NEW01300
NEW01310
NEW01320
NEW01330
NEW01340
C      C90
WRITE(NPOUT,903) R1,R2,TEMP
CONTINUE
*** INITIALIZE RA1 & RA2
RA1 = R1
RA2 = RA1+DR
C      C90
*** INDICATE TO USER HOW FAR SOLUTION FIELD HAS PROGRESSED
WRITE(6,902) R1
C      C90
*** IF RANGE STEP GREATER THAN 1 (?) WAVELENGTH WRITE WARNING
IF ( DR.LE.XLAMDA ) GO TO 90
WRITE(6,901) R1, R2, DR, XLAMDA
WRITE(NPOUT,901) R1, R2, DR, XLAMDA
C      C90
RETURN
C      C100
*** ERROR EXIT
WRITE(6,900) IBOIT?, IBOI2, IBOI1
WRITE(NPOUT,900) IBOI2, IBOI1
C      C90
STOP
C      C900
FORMAT(/,1X,'ERROR: THE RANGE AT BOTTOM PROFILE POINT NUMBER ',
*,12,' IS LESS ',9X,' THAN THE RANGE AT BOTTOM PROFILE POINT ',
*,12,' NUMBER ',12,'.',/,1X,' EXECUTION TERMINATED.',/)
C      C901
FORMAT(/,1X,'WARNING: THE HORIZONTAL RANGE STEP BETWEEN RANGE R =',F8.1,'/',
*,1X,' AND RANGE R =',F8.1,' (METERS) IS',F5.1,' METERS.',/)
*,1X,' THE REFERENCE WAVELENGTH IS',F5.1,' METERS.',/)
*,1X,' THE PROGRAM HAS REACHED RANGE R =',F8.1,' METERS.',/)
C      C902
FORMAT(/,1X,' NOTE: THE BOTTOM MODIFIED BECAUSE OF ITS AND RANGE',
*,1X,' F8.1,',9X,' HAS BEEN MODIFIED BECAUSE CF ITS VERY SMALL',
*,1X,' SLOPE.',/,9X,' THE DIFFERENCE BETWEEN THE MODIFIED',
*,1X,' BOTTOM AND YOUR',/,9X,' INPUT BOTTOM IS NEVER GREATER',
*,1X,' THAN',F5.2,' METERS.',/)
C      END

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NNEW00010  
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```

(1) COMPUTES TRI(DIAGONAL MATRIX ELEMENTS FOR MATRIX X
      (A) MATRIX Y IS AT RHS OF EQUATION FIELD IS KNOWN: RANGE=RA1
      (B) Y MATRIX ON LHS OF EQUATION WHERE: RANGE=RA1 TO
      USES Y MATRIX ELEMENTS AND KNOWN FIELD AT RANGE RA1 TO
      COMPUTES RHS COLUMN VECTOR C(I,4). (SEE TRIDG AND TEXT)
(2) COMPUTES TRI(DIAGONAL OF MATRIX X
      (A) X MATRIX ON LHS OF EQUATION
      (B) X MATRIX VALUES STORED IN C(I,1), C(I,2) AND C(I,3)
      (C) X MATRIX AT RANGE: RA1 = RA1 + DR
      (SEE TRIDG AND TEXT: RA2 = RA1 + DR
      X MATRIX AT RANGE:

```

[illegible]

```

*****
XLI,XLI2,XLRWS,XMI,XMS,XRI,XRI2,
XX1,XX2,XX3,XX6,XX7,XX8,XX9,XX12,XX1M,
YLI,YLI2,YLI3,YLRWS,YMI,YMS,YMW,YRI,YRIV,YRI2,
U,Z,Z2,Z6,Z7,Z28,Z29,Z210
/IN/IA,IBOT,I,IFACE,IPZ,ISLCPE,ISTEP,IWZ,N,NA,NBOT,NM1,
COMMON
/REAL/ALPHA,AT1(5000),BETA1,BETA2,BR(101),BZ(101),CO,
CSVP(101),C2,CWATER(5000),DR1,DR2,DR3,DR4,DR5,DR6,DR7,DR8,DR9,DR10,
R1,R1A,R1B,R1C,R1D,R1E,R1F,R1G,R1H,R1I,R1J,R1K,R1L,R1M,R1N,R1O,R1P,
XX1,X,XWR,WDR,ZLYR1,ZLYR2,ZLYR3,ZLYR4,ZLYR5,ZLYR6,ZLYR7,ZLYR8,ZLYR9,
/CPLX/A(5000),A2,A3,A4,A5,A6,A7,A8,A9,A10,A11,A12,A13,A14,A15,A16,
EYE,XLI,XLI2,XLRWS,XMI,XMS,XRI,XRI2,
XX1,XX2,XX3,XX6,XX7,XX8,XX9,XX12,XX1M(5000),
YLI,YLI2,YLI3,YLRWS,YMI,YMS,YMW,YRI,YRIV,YRI2,
U(5000),Z,Z2,Z6,Z7,Z28,Z29,Z210
COMMON
*****

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```

C C      *** COMPUTE MAIN DIAGONAL ELEMENT, Y MATRIX, IN SEDIMENT
C C      YMS = 1.0 + DR*XX3
C C      *** COMPUTE OFF-DIAGONAL ELEMENTS, Y MATRIX, IN WATER & SEDIMENT
C C      YLRWS = DR*XX1
C C      *** COMPUTE MAIN DIAGONAL ELEMENT, X MATRIX, IN SEDIMENT
C C      XMS = 2.0 - YMS
C C      *** COMPUTE OFF-DIAGONAL ELEMENTS, X MATRIX, IN WATER & SEDIMENT
C C      XLRWS = -YLRWS
C C      *** COMPUTE FIRST ELEMENT IN RHS COLUMN VECTOR
C C      YMW(1) = 1.0 + DR*XX1M(1)
C C      C(1,4) = U(1)*YMW(1) + U(2)*YLRWS
C C      *** COMPUTE TWO ELEMENTS IN FIRST ROW ON LHS
C C      C(1,2) = 2.0 - YMW(1)
C C      C(1,3) = XLRWS
C C      *** COMPUTE REMAINING ELEMENTS ON BOTH RHS & LHS FOR ROWS IN WATER
C C      IFACEN = IFACE - 1
C C      DO 10 I=2,IFACEN
C C      *** FIRST WORK WITH RHS
C C      YMW(I) = 1.0 + DR*XX1M(I)
C C      C(I,4) = U(I)*YMW(I) + (U(I-1)+U(I+1))*YLRWS
C C      *** WORK WITH LHS
C C      C(I,1) = XLRWS
C C      C(I,2) = 2.0 - YMW(I)
C C      C(I,3) = XLRWS
C C      10 CONTINUE
C C      *** COMPUTE LHS & RHS ELEMENTS IN SEDIMENT
C C      IFACEP = IFACE + 1
C C      NM1 = N - 1
C C      DO 20 I=IFACEP,NM1
C C      *** RHS
C C      C(I,4) = U(I)*YMS + (U(I-1)+U(I+1))*YLRWS
C C      *** LHS
C C      C(I,1) = XLRWS
C C      C(I,2) = XMS
C C      C(I,3) = XLRWS
C C      20 CONTINUE
C C      *** IF ENTIRE SEGMENT LEVEL GO TO 50
C C      IF ( ISLOPE.EQ.2 ) GO TO 50
C C      *** INTERFACE SLOPES EITHER UP OR DOWN
C C      *** CALCULATE CONSTANTS FOR COMPUTING MATRIX ELEMENTS
C C      THETA = ABS (THETA)
C C      SINE = SIN (THETA)
C C      COSE = COS (THETA)
C C      DELTA = XX10 + XX11*(XX8+XX9)*SINE*COSE
C C      DELIN = 1.0 / DELTA

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    BECA1 = DELIN * XX12 * RH01
    GAMMA1 = DELIN * (XX12*(RH02*CCSE*CCSE+RH01*SINE*SINE) +
    *      XX11*SINE*COSE/DZ)
    BEDA2 = DELIN * (XX12*(RH01*CCSE*CCSE+RH02*SINE*SINE) +
    *      XX11*SINE*COSE/DZ)
    GAMMA2 = DELIN * XX12 * RH02
    ZZ1 = DELIN * (RH01*SINE*SINE + RH02*COSE*COSE +
    *      XX8*SINE*COSE*XX11)
    ZZ2 = DELIN * (RH01*A2 - (COSE-XX8*SINE)*XX9*XX11*EYE*XX0*
    *      SINE)
    ZZ3 = DELIN * RH02
    ZZ4 = DELIN * ( A2 * ( RH01*CCSE*CCSE + RH02*SINE*SINE
    *      + XX8*SINE*COSE*XX11 )
    *      ( COSE + XX8*SINE ) * XX9*XX11*EYE*XX0*SINE )
    ZZ5 = 0.5*DR*ZZ1
    ZZ6 = 1.0 + 0.5*DR*(ZZ2-BEDA1-GAMMA1)
    ZZ7 = -0.5*DR*ZZ3
    ZZ8 = 1.0 - 0.5*DR*(ZZ4-BEDA2-GAMMA2)
    ZZ9 = 2.0 - ZZ8
    ZZ10 = 2.0 - ZZ6

    ** IF BOTTOM SLOPES UP, GO TO 40
    IF ( ISLOPE.EQ.3 .OR. ISLOPE.EQ.5 ) GO TO 40
    **
    ** BOTTOM SLOPES DOWN
    IFACE2 = IFACEP
    ** COMPUTE OFF-DIAGONAL, Y MATRIX ELEMENTS ON INTERFACE
    YLI = 0.5 * DR * GAMMA1
    YRI = 0.5 * DR * BEDA1
    ** COMPUTE MAIN DIAGONAL, Y MATRIX ELEMENT ON INTERFACE
    YMI = A(IFACE1) * ZZ5 + ZZ6
    ** COMPUTE INTERFACE ELEMENT IN RHS COLUMN VECTOR
    C(IFACE,4) = U(IFACEP)*YLI + U(IFACE)*YMI +
    *      U(IFACE)*YRI
    ** COMPUTE X MATRIX ELEMENTS ON INTERFACE
    XLI = -0.5*DR * GAMMA2
    XMI = A(IFACE2) * ZZ7 + ZZ8
    XRI = -0.5*DR * BEDA2
    ** IF MODIFIED BOTTOM THEN NO NEED TO ADJUST LHS
    IF ( ISLOPE.EQ.4 ) GO TO 45
    C(IFACE2,1) = XLI
    C(IFACE2,2) = XMI
    C(IFACE2,3) = XRI
    ** COMPUTE X MATRIX ELEMENTS ONE ROW ABOVE INTERFACE
    C(IFACE,1) = XLRWS
    C(IFACE,2) = 1.0 - DR * XX1M(IFACE)
    C(IFACE,3) = XLRWS
    GO TO 60
  
```

C  
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 C  
 C  
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 C  
 C  
 C  
 C

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C 40
C
*** BOTTOM SLOPES UP
IFACE2 = IFACE1
** COMPUTE OFF DR * GAMMA2
YLI = 0.5 * DR * BEDA2
YRI = 0.5 * DR * BEDA2
** COMPUTE MAIN DIAGONAL Y MATRIX ELEMENT ON INTERFACE
YMI = - A(IFACE) * ZZ1 + ZZ9
** COMPUTE INTERFACIAL ELEMENT IN RHS COLUMN VECTOR
C(IFACE,4) = U(IFACE)*YLI + U(IFACE)*YMI +
* U(IFACE)*YRI
** COMPUTE X MATRIX ELEMENTS ON INTERFACE
XLI = -0.5 * DR * GAMMA1 + ZZ10
XMI = - A(IFACE2) * ZZ5
XRI = -0.5 * DR * BEDA1
** IF MODIFIED BOTTOM THEN NO NEED TO ADJUST LHS
IF ( ISLOPE.EQ.5 ) GO TO 45
C(IFACE2,1) = XLI
C(IFACE2,2) = XMI
C(IFACE2,3) = XRI
** COMPUTE X MATRIX ELEMENTS ONE ROW BELOW INTERFACE
C(IFACE,1) = XLRWS
C(IFACE,2) = XMS
C(IFACE,3) = XLRWS
GO TO 60

C 45
C
*** SAVE INTERFACE VALUES ON SLOPING SECTION
YLI2 = YLI
YRI2 = YRI
XLI2 = XLI
XRI2 = XRI

C 50
C
*** SEGMENT LEVEL 2
IFACE2 = IFACE1
YLI = DR * XX6
YMI = 1.0 * XX7
YRI = DR * XX7
C(IFACE,4) = U(IFACE)*YLI + U(IFACE)*YMI + U(IFACE)*YRI
C(IFACE,1) = -YLI
C(IFACE,2) = -YRI
C(IFACE,3) = -YRI
** SAVE INTERFACE VALUES ON LEVEL SECTION
YLI4 = YLI
YRI4 = YRI

C 60
C
CONTINUE
*** COMPUTE ARTIFICIAL ATTENUATION MATRIX
*** SEE AISC PE MODEL BY BROCK - NORDA TECH NOTE 12 - JAN 78

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NEW01450
NEW01460
NEW01470
NEW01480
NEW01490
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NEW01580
NEW01590
NEW01600
NEW01610
NEW01620
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NEW01690
NEW01700
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NEW01800
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NEW01530
NEW01540
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NEW01670
NEW01680
NEW01690

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```

C *** CALCULATE GRID POINT AT TOP OF ART ATTENUATION LAYER
C IA = INT ( ZABLYR/DZ + 0.01 )
C *** CALCULATE NUMBER OF GRID POINTS IN ART ATTENUATION LAYER
C NA = N - IA
C *** CALCULATE ATTENUATION MATRIX
C DO 70 I=1,NA
C   TEMP = 3.0 * (1-NA) / NA
C   ATT(I) = EXP(-0.01*OR*EXP(-(TEMP*TEMP)))
C   CONTINUE
C *** SOLVE FOR SOLUTION FIELD AT RANGE RA2
C CALL TRIDG (C,U,N,CR,CTWO)
C *** APPLY ARTIFICIAL ATTENUATION
C CALL ATTENU (U,A,T,IA,NA)
C RA2P = RA2 + 0.5
C *** TIME TO WRITE?
C IF ( RA2P.GE.XWR ) CALL WRITE2
C *** TIME TO PRINT?
C IF ( RA2P.GE.XPR ) CALL PRINT2
C *** UPDATE INTERFACE POINTER
C IFACE = IFACE2
C RETURN
C END

```



TRI00490  
TRI00500

RE TURN  
END

TRI000010  
 TRI000020  
 TRI000030  
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 TRI000330  
 TRI000340  
 TRI000350  
 TRI000360  
 TRI000370  
 TRI000380  
 TRI000390  
 TRI000400  
 TRI000410  
 TRI000420  
 TRI000430  
 TRI000440  
 TRI000450  
 TRI000460  
 TRI000470

```

SUBROUTINE TRIDL (C,U,N,CR,CTWG)

*** SUBROUTINE IS A MODIFIED VERSION OF SUBROUTINE TRIDG
FROM THE IFD PROGRAM. SUBROUTINE TRIDG IS IN TURN A MODIFIED
VERSION OF TRIDG AS PER THE REFERENCE BELOW.
*** THE SUBROUTINE SOLVES A SET OF N - 1 (NM1) LINEAR
SIMULTANEOUS EQUATIONS HAVING A TRIANGULAR COEFFICIENT
MATRIX. MATRIX ELEMENTS IN THE LOWER DIAGONAL, MAIN DIAGONAL
AND UPPER DIAGONAL ARE STORED IN C(I,1), C(I,2) AND C(I,3)
RESPECTIVELY. THE RHS COLUMN VECTOR IS STORED IN C(I,4).
THE SOLUTION FIELD IS STORED IN U(I).
*** THE INDEX I REFERS TO ROW NUMBER. SYSTEM (RATHER THAN
WE NEED ONLY SOLVE AN NM1 X NM1 SYSTEM BECAUSE U(N)=0.0
AN NM1 X N SYSTEM IS A MODIFIED VERSION OF IFD SUB-
ROUTINE TRIDG WHICH IN TURN IS A MODIFIED VERSION
OF SUBROUTINE TRIDG AS PER:
*** "APPLIED NUMERICAL ANALYSIS" (SECOND EDITION)
BY: CURTIS F. GERALD
PUBLISHED BY ADDISON-WESLEY PUBLISHING CO., 1980
*** THE ONLY MODIFICATION TO IFD SUBROUTINE TRIDG IS
THAT TRIDL DOES NOT RECALCULATE CTWO AND CR, BUT
BUT TRIDL USES THE ARRAY VALUES CALCULATED
BY TRIDG. THIS RESULTS IN A CONSIDERABLE SAVINGS
IN EXECUTION TIME FOR THE CASE OF A HORIZONTAL
BOTTOM.

COMPLEX C(5000,4), U(5000), CR(5000), CTWO(5000)

NM1 = N - 1
NM2 = N - 2
DO 10 I=2,NM1
  C(I,4) = C(I,4) - CR(I) * C(I-1,4)
CONTINUE

U(N) = 0.0

*** NOW PERFORM BACK SUBSTITUTION

U(NM1) = C(NM1,4) / CTWG(NM1)
DO 20 I=1,NM2
  M = NM1 - I
  U(M) = ( C(M,4) - C(M,3)*U(M+1) ) / CTWG(M)
CONTINUE

RETURN
END
  
```

CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC C

10 C

CC C

20 C



DDW0C490  
DDW00500  
DDW0C510  
DDW0C520

C    \*\*\* UPDATE IFACE  
      IFACE = IFACE2  
      RETURN  
      END



DOW00010  
 DOW00020  
 DOW00030  
 DOW00040  
 DOW00050  
 DOW00060  
 DOW00070  
 DOW00080  
 DOW00090  
 DOW00100  
 DOW00110  
 DOW00120  
 DOW00130  
 DOW00140  
 DOW00150  
 DOW00160  
 DOW00170  
 DOW00180  
 DOW00190  
 DOW00200  
 DOW00210  
 DOW00220  
 DOW00230  
 DOW00240  
 DOW00250  
 DOW00260  
 DOW00270  
 DOW00280  
 DOW00290  
 DOW00300  
 DOW00310  
 DOW00320  
 DOW00330  
 DOW00340  
 DOW00350  
 DOW00360  
 DOW00370  
 DOW00380  
 DOW00390  
 DOW00400  
 DOW00410  
 DOW00420  
 DOW00430  
 DOW00440  
 DOW00450  
 DOW00460  
 DOW00470  
 DOW00480

# SUBROUTINE DOWN

THIS SUBROUTINE UPDATES THE RHS & LHS OF THE EQUATION AND  
 SOLVES FOR THE SOLUTION VECTOR FIELD AT RA2.  
 (1) THE RHS COLUMN VECTOR VALUES ARE STORED IN C(I,4)  
 (2) THE INTERFACE AT RANGE RA1 IS AT GRIDPOINT IFACE  
 (3) THE INTERFACE AT RANGE RA2 IS AT GRIDPOINT IFACE2  
 ( WHERE IFACE2 = IFACE + 1 )

```

COMPLEX A,A2,C,CR,CTWO,EYE,XMS,XRI,XRIZ,
* XLI,XLIZ,XLRWS,XMI,XX6,XX7,XX8,XX9,XX12,XX1M,
* XX1,XX2,XX3,XX4,XX5,XX6,XX7,XX8,XX9,XX12,XX1M,
* YLI,YLIV,YLIZ,YLRWS,YMI,YMS,YMW,YRI,YRIV,YRIZ,
* U,Z,Z5,ZZ6,ZZ7,ZZ8,ZZ9,ZZ10
COMMON /IN/ IA,I80,T1,IFACE,IPZ,ISLOPE,ISTEP,IMZ,N,NA,NBOT,NM1,
* NSTEP,NSTEP1,NSVP,NHMAX,NX1,IFS
COMMON /REAL/ ALPHA,ATT(5000),BETA1,BETA2,BR(101),BZ(101),CO,
* R1,RAI,RA2,RHDI,PHD2,RMAX,THETA,XKO,XLANDA,XPR,XX4,XX10,
* XX11,XWMR,WDR,ZLYR1,ZLYR2,ZR,ZS,ZSVP(101),ZABLYR
COMMON /CPLX/ A(5000),A2,C(5000,4),CR,XRI,XRIZ,
* EYE,XLI,XLIZ,XLRWS,XMI,XX6,XX7,XX8,XX12,XX1M(5000),
* XX1,XX2,XX3,XX4,XX5,XX6,XX7,XX8,XX12,XX1M(5000),YRIZ,
* YLI,YLIV,YLIZ,YLRWS,YMI,YMS,YMW(5000),YRI,YRIV,YRIZ,
* U(5000),Z25,Z26,Z27,Z28,Z29,ZZ10
  
```

```

*** UPDATE IFACE2
IFACE2 = IFACE + 1
*** UPDATE Y MATRIX X, MAIN DIAGONAL, INTERFACE ELEMENT
YMI = A( IFACE ) * ZZ5 + ZZ6
*** UPDATE Y MATRIX X, MAIN DIAGONAL, WATER ELEMENT, ONE ROW
ABOVE INTERFACE
YMW( IFACE-1 ) = 1.0 + DR * XX1M( IFACE-1 )
  
```

```

*** UPDATE RHS
CALL RHS
*** UPDATE LHS
*** ** UPDATE X MATRIX ELEMENTS ONE ROW ABOVE INTERFACE
C( IFACE,1 ) = XLRWS
C( IFACE,2 ) = 1.0 - DR * XX1M( IFACE )
C( IFACE,3 ) = XLRWS
*** ** UPDATE X MATRIX ELEMENTS ON INTERFACE
C( IFACE2,1 ) = XLI
C( IFACE2,2 ) = A( IFACE2 ) * ZZ7 + ZZ8
C( IFACE2,3 ) = XRI
  
```

```

*** SOLVE THE TRIDIAGONAL SYSTEM
CALL TRIDG (C,U,N,CR,CTWO)
  
```

DOW00490  
DOW00500  
DOW00510  
DOW00520

\*\*\* UPDATE IFACE  
IFACE = IFACE2  
RETURN  
END

C



```

SUBROUTINE SSLOPE
*** THIS SUBROUTINE IS CALLED TO ADVANCE THE SOLUTION FIELD
*** FOR THE CASE OF A MODIFIED BOTTOM.
*** (1) THIS CASE OCCURS WHEN THE BOTTOM SLOPE IS TOO SMALL
*** FOR THE MAXIMUM RANGE STEP.
*** (2) THIS SUBROUTINE WORKS FOR BOTH A DOWNSLOPE AND
*** UPSLOPE MODIFIED BOTTOM.
*** (3) THE SUBROUTINE DETERMINES WHICH OF THE FOLLOWING
*** THREE TYPES OF BOTTOM SECTIONS NEEDS TO BE CONSIDERED:
*** (A) LEVEL SECTION FOLLOWS LEVEL SECTION
*** (B) LEVEL SECTION FOLLOWS SLOPING SECTION
*** (C) SLOPING SECTION.
*** (4) AFTER DETERMINING WHICH OF THE THREE TYPES OF BOTTOM
*** SECTIONS IS APPROPRIATE, THE SUBROUTINE MAKES MATRIX
*** ELEMENT CHANGES AS REQUIRED AND CALLS ON OTHER
*** SUBROUTINES TO ADVANCE THE SOLUTION.

COMPLEX A,A2,C,CR,CTWO,EYE,XLI,XL12,XLRWS,XMI,XMS,XRI,XRIZ,
* XL1,XX2,XX3,XX4,XX5,XX6,XX7,XX8,XX9,XX12,XX1M,
* YLI,YL12,YL13,YL14,YL15,YL16,YL17,YL18,YL19,YL20,YL21,
* U,Z,Z5,Z6,Z7,Z8,Z9,Z10,Z11,Z12,Z13,Z14,Z15,Z16,Z17,Z18,Z19,Z20,
* /IN/ IA,IBOT,IFACE,IPZ,ISLOPE,ISTEP,IWZ,N,NA,NBOT,NM1,
* NSTEP,NSTEP1,NSTEP2,NSTEP3,NSTEP4,NSTEP5,NSTEP6,NSTEP7,
* /REAL/ ALPHA,A1,A2,A3,A4,A5,A6,A7,A8,A9,A10,A11,A12,A13,A14,A15,
* /CSVF/ (101),C2,CWATER(5000),BETA1,BETA2,BR101,BZ101,CO,
* R1,RAL,RA2,RH01,RH02,RMAX,THETA,XK0,XLAMD,XPR,XX4,XX10,
* XX11,XXWR,WDR,ZLYR1,ZLYR2,ZR,ZS,ZSVP(101),ZABLYR,
* /CPLX/ A(5000),A2,C(5000,4),CR(5000),CTWO(5000),
* EYE,XL1,XL12,XLRWS,XMI,XMS,XRI,XRIZ,
* XL1,XX2,XX3,XX4,XX5,XX6,XX7,XX8,XX9,XX12,XX1M(5000),
* YLI,YL12,YL13,YL14,YL15,YL16,YL17,YL18,YL19,YL20,YL21,
* U(5000),Z5,Z6,Z7,Z8,Z9,Z10,Z11,Z12,Z13,Z14,Z15,Z16,Z17,Z18,Z19,Z20,

*** IS THIS A LEVEL SECTION FOLLOWING A SLOPING SECTION?
IF (ISTEP.EQ.NXLFS) GO TO 20
*** NO

*** IS THIS A SLOPING SECTION?
ITEST = NXLFS - ISTEP
IF (ITEST.EQ.1) GO TO 30
*** NO

*** LEVEL SECTION FOLLOWS A LEVEL SECTION
CALL LEVEL
GO TO 50

```

CCCCCCCCCCCCCCCC

CC CCC CCCC C

```

C 20 *** LEVEL SECTION FOLLOWS A SLOPING SECTION
C *** UPDATE NXLF S
C *** NXLF S = NXLF S + NSTEP1
C *** IF LAST SECTION SLOPED DOWN, UPDATE Y MATRIX ELEMENT,
C *** MAIN DIAGONAL IN WATER, ONE ROW ABOVE INTERFACE
C IF ( ISLOPE.EQ.5 ) GO TO 25
C YMH( IFACE-1 ) = 1.0 + DR * XXIM( IFACE-1 )
C *** UPDATE RHS INTERFACE ELEMENTS
C YLI = YLIV + DR * ( XXIM( IFACE ) / XX4 + XX5 )
C YRI = YRIV
C *** UPDATE LHS
C C( IFACE, 1 ) = -YLI
C C( IFACE, 2 ) = 2.0 - YMI
C C( IFACE, 3 ) = -YRI
C *** SOLVE SYSTEM
C CALL RHS
C CALL TRIDG( C, U, N, CR, CTWO )
C GO TO 50
C *** SLOPING SECTION
C *** UPDATE INTERFACE ELEMENTS
C YLI = YLIZ
C YRI = YRIZ
C XLI = XLI
C XRI = XRI
C *** SOLVE SYSTEM AS APPROPRIATE
C IF ( ISLOPE.EQ.4 ) CALL DOWN
C IF ( ISLOPE.EQ.5 ) CALL UP
C 50 CONTINUE
C RETURN
C END

```

```

SSL00490
SSL00500
SSL00510
SSL00520
SSL00530
SSL00540
SSL00550
SSL00560
SSL00570
SSL00580
SSL00590
SSL00600
SSL00610
SSL00620
SSL00630
SSL00640
SSL00650
SSL00660
SSL00670
SSL00680
SSL00690
SSL00700
SSL00710
SSL00720
SSL00730
SSL00740
SSL00750
SSL00760
SSL00770
SSL00780
SSL00790
SSL00800
SSL00810

```









PRI00490  
PRI00500  
PRI00510

RETURN  
END

C

WRI000010  
 WRI000020  
 WRI000030  
 WRI000040  
 WRI000050  
 WRI000060  
 WRI000070  
 WRI000080  
 WRI000090  
 WRI000100  
 WRI000110  
 WRI000120  
 WRI000130  
 WRI000140  
 WRI000150  
 WRI000160  
 WRI000170  
 WRI000180  
 WRI000190  
 WRI000200  
 WRI000210  
 WRI000220  
 WRI000230  
 WRI000240  
 WRI000250  
 WRI000260  
 WRI000270  
 WRI000280  
 WRI000290  
 WRI000300  
 WRI000310  
 WRI000320  
 WRI000330  
 WRI000340  
 WRI000350  
 WRI000360

```

SUBROUTINE WRITE2
(1) THIS SUBROUTINE IS EFFECTIVELY THE CONTINUATION OF
    SUBROUTINE WRITE1
(2) THE SUBROUTINE WRITES RANGE, RECEIVER DEPTH AND U(1)
    WHEN CALLED. IT THEN UPDATES THE NEXT WRITE RANGE (XWR)
(3) THE FILE WRITTEN INTO CORRESPONDS TO UNIT FILE NUMBER:
    NOU = 52
(4) THE FILENAME AND FILETYPE FOR THIS FILE ARE:
    THE IFDOUT PLOTTER

COMPLEX A,A2,C,CR,CTMG,EYE,XMS,XRI,XRIZ,
* XL1,XLIZ,XLRWS,XMI,XMS,XRI,XRIZ,
* XX1,XX2,XX3,XX4,XX5,XX6,XX7,XX8,XX9,XX12,XX1M,
* YL1,YLIV,YLIZ,YLRWS,YMI,YMS,YMW,YRI,YRIV,YRIZ,
* U,Z,Z5,ZZ6,ZZ7,ZZ8,ZZ9,ZZ10
COMMON /IN/ IA,IBOT,IFACE,IP1,ISLGPE,ISTEP,IMZ,N,NA,NBOT,NML,
* NSTEP,NSTEP1,NSVP,NMMA,X,NXLFS
COMMON /REAL/ ALPHA,ATT(5000),BETA1,BETA2,BR(101),BZ(101),CO,
* R1,FA1,RA2,RH01,RH02,RMAX,THEIA,XK0,XLAMD,A,XPR,XX4,XX10,
* XX11,XMR,MOR,ZLVR1,ZLVR2,ZR,ZS,ZSVP(101),ZABLYR
COMMON /CPLX/ A(5000),A2,XLRWS,XMI,XMS,XRI,XRIZ,
* EYE,XL1,XLIZ,XLRWS,XMI,XMS,XRI,XRIZ,XX1,XX2,XX3,XX4,XX5,XX6,XX7,XX8,XX9,XX12,XX1M(5000),
* XL1,XX2,XX3,XX4,XX5,XX6,XX7,XX8,XX9,XX12,XX1M(5000),YMI,YMS,YMW(5000),YRI,YRIV,YRIZ,
* U(5000),Z5,ZZ6,ZZ7,ZZ8,ZZ9,ZZ10
DATA NOU/52/

*** WRITE RANGE, DEPTH AND U(1)
WRITE(NCU,*) RA2,ZR,U(1M)

*** DETERMINE NEXT RANGE AT WHICH TO WRITE SOLUTION
XWR = XWR+PDR
RETURN
  
```

CCCCCCCCCCCC

CC C C C

IFDI 5850  
 IFDI 5860  
 IFDI 5870  
 IFDI 5880  
 IFDI 5890  
 IFDI 5900  
 IFDI 5910  
 IFDI 5920  
 IFDI 5930  
 IFDI 5940  
 IFDI 5950  
 IFDI 5960  
 IFDI 5970  
 IFDI 5980  
 IFDI 5990  
 IFDI 6000  
 IFDI 6010

```

SUBROUTINE ATTENU(U,ATT,IA,NA)
THIS SUBROUTINE APPLIES ARTIFICIAL ATTENUATION TO THE BOTTOM-
MOST NA GRID POINTS AS PER AESD PE MODEL BY BROCK - NORDA
TECH NOTE 12 - JAN 78
(1) ATTENUATION MATRIX ATT IS CALCULATED IN SUBROUTINE
    NEWMAT
COMPLEX U(5000)
DIMENSION ATT(5000)
DO 10 I=1,NA
  U(IA+I) = U(IA+I) * ATT(I)
CONTINUE
RETURN
END

```

CCCCCCC

C

10

C



## APPENDIX B

### RUNNING THE IMPLICIT FINITE-DIFFERENCE PROGRAM ON THE NPS COMPUTER

#### A. INTRODUCTION

This appendix describes one simple procedure for running the IFD program on the NPS computer.

#### B. COPYING FILES ONTO USER'S DISK

Four files are needed to run the IFD program; the filenames and filetypes are

IFD	FORTRAN
IFD	EXEC
PLOTIFD	FORTRAN
PLOTIFD	EXEC

The files are available from a computer account maintained by the underwater acoustics curriculum. To link with this account and obtain copies of the files the user should proceed as follows:

- (1) Log on terminal
- (2) Enter: CP LINK 0160P 191 195 RR
- (3) When prompted for read password enter: UX
- (4) Enter: ACC 195 C
- (5) Enter: COPYIFD

At this point the four files should reside on the user's A disk.

### C. RUNNING THE IFD PROGRAM

Before running the IFD program the user should define additional storage space, compile the program, and set up the input data file. To define additional storage space,

- (1) Enter: DEF STOR 1M
- (2) Enter: I CMS

These two commands need only be entered one time for each terminal session; the storage space will remain for the entire session.

To compile the program,

Enter: FORTGI IFD

The program need be compiled only one time unless the program is changed, in which case the new version should be recompiled.

The final step before running the program is setting up the input data file which has filename and filetype IFDIN DATAIN. The user must create or modify this file so that it contains input data as described in Section III.E.2 of this thesis. For more information concerning how to create or modify files see NPS Technical Note TN-VM-02 which is available in the computer consultant's office.

If the above steps are accomplished, the user can then run the program with

Enter: IFD

Shortly after entering this command the user will be prompted for a run identification. The run identification

is an arbitrary identification label that will appear on the output printer file. Enter run identification as desired.

At the end of the run the user is informed of the two output data files generated by the program. If desired by the user the output printer file (IFDOUT PRINTER) may be sent to the printer. The output plotter file, IFDOUT PLOTTER, serves as an input file for the plotting program.

#### D. RUNNING THE PLOTTING PROGRAM

A Tektronix-618 terminal is used to run the plotting program. The first step is to log onto the terminal in the normal manner and then define additional storage space by,

- (1) Enter: DEF STOR 1M
- (2) Enter: I CMS

The plotting program has filename and filetype PLOTIFD FORTRAN. To compile the program,

Enter: FORTGI PLOTIFD

Unless the program is changed it need only be compiled one time. To run the program

Enter: PLOTIFD

The user will be prompted for axes and smoothing information; enter values and responses as appropriate. The transmission loss curve will be displayed on the CRT screen, a hard copy may be obtained by pushing the HARD COPY button under the screen, and the screen may be cleared by pushing the ENTER key.

FL0000010  
FL0000020  
FL0000030  
FL0000040  
FL0000050  
FL0000060  
FL0000070  
FL0000080  
FL0000090  
FL0000100  
FL0000110  
FL0000120  
FL0000130  
FL0000140  
FL0000150  
FL0000160  
FL0000170  
FL0000180  
FL0000190  
FL0000200  
FL0000210  
FL0000220  
FL0000230  
FL0000240  
FL0000250  
FL0000260  
FL0000270  
FL0000280  
FL0000290  
FL0000300  
FL0000310  
FL0000320  
FL0000330  
FL0000340  
FL0000350  
FL0000360  
FL0000370  
FL0000380  
FL0000390  
FL0000400  
FL0000410  
FL0000420  
FL0000430  
FL0000440  
FL0000450  
FL0000460  
FL0000470  
FL0000480

10



```

C 20
*** REAL SOLUTION FIELD
    REAC(NOC,*,END=40) RA, ZR, U
    IF (RA.LE.0.0) GO TO 20
    L = L + 1
    P(L) = CABS(U)
    R(L) = RA
    GO TO 20
C 40
CONTINUE
IF (NPCINT.EQ.0) GO TO 70
C
*** THIS SECTION SMOOTHS THE DATA
    L = L - NPCINT + 1
    DO 60 I=1,L
        PTEMP = 0.0
        RTEMP = 0.0
        DO 50 J=1,NPCINT + P(I+J-1)
            PTEMP = PTEMP + P(I+J-1)
            RTEMP = RTEMP + R(I+J-1)
        CONTINUE
        P(I) = PTEMP / FLOAT(NPCINT)
        R(I) = RTEMP / FLOAT(NPCINT)
    CONTINUE
C
*** CALCULATE VALUES TO BE PLOTTED
    NOTE: THE TRANSMISSION LOSS VALUES CALCULATED
    BELOW ARE THE INVERSE SIGN OF THE TRUE TL VALUES
    THIS IS DONE SO THAT HIGHER TL VALUES TEND
    TOWARDS THE MINUS Y DIRECTION.
C 50
C 60
C 70
DO 80 I=1,L
    P(I) = 20.0*ALOG10(P(I)) - 10.0*ALOG10(R(I))
    R(I) = R(I) / 1000.0
CONTINUE
C 80
CALL TEK618
CALL NCBRR(14.0,10.0)
CALL PAGE(13.5,2.9)
CALL PHYSOR(10.0,6.7)
CALL AREA2D(.25)
CALL HEIGHTS(2)
CALL VTICKS(2)
CALL XNAME('RANGE (KM)',100)
CALL YNAME('PROPAGATION LOSS (DB)',100)
CALL HEADIN('THIS IS A HEADINGS',100,1.2,2)
CALL GRAF (X1,X2,X3,Y1,Y2,Y3)
CALL CUFVE(F,P,L,0)

```

```

PL0000490
PL0000500
PL0000510
PL0000520
PL0000530
PL0000540
PL0000550
PL0000560
PL0000570
PL0000580
PL0000590
PL0000600
PL0000610
PL0000620
PL0000630
PL0000640
PL0000650
PL0000660
PL0000670
PL0000680
PL0000690
PL0000700
PL0000710
PL0000720
PL0000730
PL0000740
PL0000750
PL0000760
PL0000770
PL0000780
PL0000790
PL0000800
PL0000810
PL0000820
PL0000830
PL0000840
PL0000850
PL0000860
PL0000870
PL0000880
PL0000890
PL0000900
PL0000910
PL0000920
PL0000930
PL0000940
PL0000950
PL0000960

```

```

C          CALL ENDPL(C)
C          CALL DCNEPL
C          STOP
C 900      FORMAT(/, 'THE X-AXIS IS ON THE FORTHCOMING TRANSMISSION LOSS CURVE RANGES', /
*          * , 'FROM RANGE R = 0.0 KM TO RANGE R =', F5.1, ' KM.', /
*          * , 'ENTER DESIRED X-AXIS INCREMENT:', /
901      FORMAT(/, 'ENTER LOWEST DB LOSS VALUE ON Y-AXIS:', /
902      FORMAT(/, 'ENTER HIGHEST DB LOSS VALUE ON Y-AXIS:', /
903      FORMAT(/, 'THE Y-AXIS ON THE TL CURVE WILL RANGE FROM A DB LOSS OF', F6.1,
*          * , ' DB.', /, 'ENTER DESIRED Y-AXIS INCREMENT:', /
904      FORMAT(/, 'DO YOU WANT THE DATA SMOOTHED? ( ENTER: Y OR N ),', /
905      FORMAT(A1)
906      FORMAT(/, 'HOW MANY POINTS DO YOU WANT AVERAGED AT EACH STEP TO ', /
*          * , 'OBTAIN SMOOTHING?', /, ' ( ENTER: 2 OR 3 OR ... ),', /
*          * END
PL000970
PL000980
PL000990
PL001000
PL001010
PL001020
PL001030
PL001040
PL001050
PL001060
PL001070
PL001080
PL001090
PL001100
PL001110
PL001120
PL001130
PL001140
PL001150

```

# APPENDIX D

## EXAMPLE OF IMPLICIT FINITE-DIFFERENCE PRINTED OUTPUT

```

IFD PRINTED CUTPLT
RUN I.D. : RUN 30, DEEP-TO-SHALLOW WATER, 8.5 DEG.

    GAUSSIAN STARTING FIELD
    (FOR FURTHER INFORMATION ON VARIABLES SEE MAIN IFD PROGRAM LISTING)

FREQUENCY          FRQ      = 25.00 HZ
SOURCE DEPTH       ZS       = 25.00 M
RECEIVER DEPTH     ZR       = 25.00 M
DEPTH INCREMENT    DZ       = 1.00 M
REF SOUND SPEED    CO       = 1500.00 M/S
REF WAVE NUMBER    XKO      = 0.10 1/M
REF WAVELENGTH     XLAMDA   = 60.00 M
MAX RANGE CF SOLUTION
RANGE STEP ON HORIZONTAL SECTION
MAXIMUM RANGE STEP
RECORDED RANGE STEP
DEPTH CF UPPER EDGE ART ATTENU LYR
#VERTICAL FOINTS IN GRID

```

```

SOUND SPEED PRGFILE IN WATER:
DEPTH          SOUND SPEED
0.0 M          1500.00 M/S

```

	350.00 M	1500.00 M/S	
LAYER	MAX DEPTH(M)	DENSITY(G/CM**3)	ATT(DB/ML)
WATER	350.0	1.00	0.000004
SEDIMENT	1600.0	1.50	0.200000
			1600.00
			SEE PROFILE ABOVE

# BOTTOM PROFILE:

RANGE	DEPTH
0.0 M	350.0 M
10000.0 M	350.0 M
12000.0 M	50.0 M
40000.0 M	50.0 M

RANGE = 10000.0 M

DEPTH	LOSS(DB)	U(1)
50.00	61.70	( 0.77277E-02
100.00	86.33	(-0.48267E-02
150.00	82.62	(-0.71538E-02
200.00	77.90	( 0.12576E-01
250.00	85.01	( 0.45182E-02
300.00	67.84	(-0.40433E-01
350.00	66.93	(-0.44474E-01
400.00	77.05	(-0.13282E-01
450.00	86.86	(-0.34990E-02
		0.28103E-02)
		-0.82565E-04)
		-0.18895E-02)
		0.19843E-02)
		0.33360E-02)
		-0.33553E-02)
		-0.71566E-02)
		-0.45756E-02)
		-0.28944E-02)

DEPTH	LOSS(DB)	U(1)	U(2)
500.00	97.76	-0.0	0.0
550.00	112.53	-0.0	0.0
600.00	97.76	-0.0	0.0
650.00	97.76	-0.0	0.0
700.00	97.76	-0.0	0.0
750.00	97.76	-0.0	0.0
800.00	97.76	-0.0	0.0
850.00	97.76	-0.0	0.0
900.00	97.76	-0.0	0.0
950.00	97.76	-0.0	0.0
1000.00	97.76	-0.0	0.0

RANGE = 2000C.0 M

DEPTH	LOSS(DB)	U(1)	U(2)
50.00	54.53	0.0	0.0
100.00	98.62	0.0	0.0
150.00	102.38	0.0	0.0
200.00	105.57	0.0	0.0
250.00	110.54	0.0	0.0
300.00	115.50	0.0	0.0
350.00	119.50	0.0	0.0
400.00	123.50	0.0	0.0
450.00	127.50	0.0	0.0
500.00	131.50	0.0	0.0
550.00	135.50	0.0	0.0
600.00	139.50	0.0	0.0
650.00	143.50	0.0	0.0
700.00	147.50	0.0	0.0
750.00	151.50	0.0	0.0
800.00	155.50	0.0	0.0
850.00	159.50	0.0	0.0
900.00	163.50	0.0	0.0
950.00	167.50	0.0	0.0
1000.00	171.50	0.0	0.0

RANGE = 3000C.0 M

DEPTH	LOSS(DB)	U(1)	U(2)
50.00	112.30	-0.0	0.0
100.00	116.30	-0.0	0.0
150.00	121.09	-0.0	0.0



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